M4RIE

0.20130416

Generated by Doxygen 1.8.4

Mon Aug 19 2013 01:13:59

Contents

1 Main Page

M4RIE is a library to do fast compations with dense matrices over $\mathbb{F}_{2^e}$ for small e. M4RIE is available under the GPLv2+.

The two fundamental data types of this library are mzed_t and mzd_slice_t. For big matrices, i.e., those which do not fit into L2 cache, it is recommended to use mzd_slice_t and for smaller matrices mzed_t will be slightly faster and use less memory.
Function names follow the pattern

```
[_]_[type]_[what]_[algorithm]
```

Function names beginning with an underscore perform less consistency checks (matching dimensions, matching fields) than those without, e.g., _mzed_ple() is called by mzed_ple() after some checks were performed.

For both data types almost all functions are the same, e.g., there is a function mzd_slice_add() and there also should be a function mzed_add() with the same signature except for the matrix type.

Functions which do not specify an algorithm choose the best available algorithm (based on some heuristic), e.g., mzed-_ple() might call mzed_ple_newton_john().

2 Todo List

Global _mzd_slice_mul_karatsuba8 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)
reduce memory requirements by writing formula explicitly

Global gf2e_t16_init (const gf2e ∗ff, const word a)

: this is a bit of overkill, we could do better

Global mzd_poly_randomize (mzd_poly_t ∗A)

Allow the user to provide a RNG callback.

Global mzd_slice_add_elem (mzd_slice_t ∗A, const rci_t row, const rci_t col, word elem)

This function is considerably slower than it needs to be.

Global mzd_slice_randomize (mzd_slice_t ∗A)

Allow the user to provide a RNG callback.

Global mzd_slice_read_elem (const mzd_slice_t ∗A, const rci_t row, const rci_t col)

This function is considerably slower than it needs to be.

Global mzd_slice_write_elem (mzd_slice_t ∗A, const rci_t row, const rci_t col, word elem)

This function is considerably slower than it needs to be.

Global mzed_echelonize_newton_john (mzed_t ∗A, int full)

we don't really compute the upper triangular form yet, we need to implement _mzed_gauss_submatrix() and a better table creation for that.

Global mzed_randomize (mzed_t ∗A)

Allow the user to provide a RNG callback.

3 Module Documentation

3.1 Type definitions

Data Structures

- struct mzd_slice_t

  Dense matrices over $\mathbb{F}_{2^e}$ represented as slices of matrices over $\mathbb{F}_2$.
- struct mzed_t

  Dense matrices over $\mathbb{F}_{2^e}$ represented as packed matrices.

3.1.1 Detailed Description

3.2 Constructions

Functions

- mzed_t ∗ mzed_cling (mzed_t ∗A, const mzd_slice_t ∗Z)

  Pack a bitslice matrix into a packed represenation.
- mzd_slice_t ∗ mzed_slice (mzd_slice_t ∗A, const mzed_t ∗Z)

  Unpack the matrix Z into bitslice representation.
- static mzd_slice_t ∗ mzd_slice_init (const gf2e ∗ff, const rci_t m, const rci_t n)

  Create a new matrix of dimension $m \times n$ over ff.
- static void mzd_slice_free (mzd_slice_t ∗A)

  Free a matrix created with mzd_slice_init().
- static mzd_slice_t ∗ mzd_slice_concat (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  Concatenate B to A and write the result to C.
- static mzd_slice_t ∗ mzd_slice_stack (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  Stack A on top of B and write the result to C.
- static mzd_slice_t ∗ mzd_slice_submatrix (mzd_slice_t ∗S, const mzd_slice_t ∗A, const size_t lowr, const size_t lowc, const size_t highr, const size_t highc)

  Copy a submatrix.
- static mzd_slice_t ∗ mzd_slice_init_window (const mzd_slice_t ∗A, const size_t lowr, const size_t lowc, const size_t highr, const size_t highc)

  Create a window/view into the matrix M.
- static void mzd_slice_free_window (mzd_slice_t ∗A)

  Free a matrix window created with mzd_slice_init_window().
- mzed_t ∗ mzed_init (const gf2e ∗ff, const rci_t m, const rci_t n)

  Create a new matrix of dimension m x n over ff.
- void mzed_free (mzed_t ∗A)

  Free a matrix created with mzed_init().
- static mzed_t ∗ mzed_concat (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  Concatenate B to A and write the result to C.
- static mzed_t ∗ mzed_stack (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  Stack A on top of B and write the result to C.
- static mzed_t ∗ mzed_submatrix (mzed_t ∗S, const mzed_t ∗M, const rci_t lowr, const rci_t lowc, const rci_t highr, const rci_t highc)

  Copy a submatrix.
- static mzed_t ∗ mzed_init_window (const mzed_t ∗A, const rci_t lowr, const rci_t lowc, const rci_t highr, const rci_t highc)

  Create a window/view into the matrix A.
- static void mzed_free_window (mzed_t ∗A)

  Free a matrix window created with mzed_init_window().

3.2.1 Detailed Description

3.2.2 Function Documentation

3.2.2.1 static mzd_slice_t∗ mzd_slice_concat (mzd_slice_t ∗ *C*, const mzd_slice_t ∗ *A*, const mzd_slice_t ∗ *B*) [inline], [static]

Concatenate B to A and write the result to C.

That is,

```
[ A ], [ B ] -> [ A  B ] = C
```

The inputs are not modified but a new matrix is created.

Parameters

C	Matrix, may be NULL for automatic creation.
A	Matrix.
B	Matrix.

Note

This is sometimes called augment.

3.2.2.2 static void mzd_slice_free (mzd_slice_t ∗ *A*) [inline], [static]

Free a matrix created with mzd_slice_init().

Parameters

A	Matrix.

3.2.2.3 static void mzd_slice_free_window (mzd_slice_t ∗ *A*) [inline], [static]

Free a matrix window created with mzd_slice_init_window().

Parameters

A	Matrix

3.2.2.4 static mzd_slice_t∗ mzd_slice_init (const gf2e ∗ *ff*, const rci_t *m*, const rci_t *n*) [inline], [static]

Create a new matrix of dimension $m \times n$ over ff.

Use mzd_slice_free() to free it.

Parameters

ff	Finite field
m	Number of rows
n	Number of columns

3.2.2.5 static mzd_slice_t∗ mzd_slice_init_window (const mzd_slice_t ∗ *A*, const size_t *lowr*, const size_t *lowc*, const size_t *highr*, const size_t *highc*) [inline], [static]

Create a window/view into the matrix M.

A matrix window for M is a meta structure on the matrix M. It is setup to point into the matrix so M *must not* be freed while the matrix window is used.

This function puts the restriction on the provided parameters that all parameters must be within range for M which is not currently enforced.

Use mzd_slice_free_window() to free the window.

Parameters

A	Matrix
lowr	Starting row (inclusive)
lowc	Starting column (inclusive)
highr	End row (exclusive)
highc	End column (exclusive)

3.2.2.6 static mzd_slice_t* mzd_slice_stack (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*) [inline], [static]

Stack A on top of B and write the result to C.

That is,

```
[ A ], [ B ] -> [ A ] = C
                [ B ]
```

The inputs are not modified but a new matrix is created.

Parameters

C	Matrix, may be NULL for automatic creation
A	Matrix
B	Matrix

3.2.2.7 static mzd_slice_t* mzd_slice_submatrix (mzd_slice_t * *S*, const mzd_slice_t * *A*, const size_t *lowr*, const size_t *lowc*, const size_t *highr*, const size_t *highc*) [inline], [static]

Copy a submatrix.

Parameters

S	Preallocated space for submatrix, may be NULL for automatic creation.
A	Matrix
lowr	start rows
lowc	start column
highr	stop row (this row is *not* included)
highc	stop column (this column is *not* included)

3.2.2.8 mzed_t* mzed_cling (mzed_t * *A*, const mzd_slice_t * *Z*)

Pack a bitslice matrix into a packed represenation.

Parameters

A	Matrix over $\mathbb{F}_{2^e}$ or NULL
Z	Bitslice matrix over $\mathbb{F}_{2^e}$

3.2.2.9 static mzed_t* mzed_concat (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*) [inline], [static]

Concatenate B to A and write the result to C.

That is,

```
[ A ], [ B ] -> [ A  B ] = C
```

The inputs are not modified but a new matrix is created.

Parameters

C	Matrix, may be NULL for automatic creation
A	Matrix
B	Matrix

Note

This is sometimes called augment.

3.2.2.10 void mzed_free (mzed_t * *A*)

Free a matrix created with mzed_init().

Parameters

A	Matrix

3.2.2.11 static void mzed_free_window (mzed_t * *A*) [inline], [static]

Free a matrix window created with mzed_init_window().

Parameters

A	Matrix

3.2.2.12 mzed_t* mzed_init (const gf2e * *ff*, const rci_t *m*, const rci_t *n*)

Create a new matrix of dimension m x n over ff.

Use mzed_free() to kill it.

Parameters

ff	Finite field
m	Number of rows
n	Number of columns

3.2.2.13 static mzed_t* mzed_init_window (const mzed_t * *A*, const rci_t *lowr*, const rci_t *lowc*, const rci_t *highr*, const rci_t *highc*) [inline], [static]

Create a window/view into the matrix A.

A matrix window for A is a meta structure on the matrix A. It is setup to point into the matrix so M *must not* be freed while the matrix window is used.

This function puts the restriction on the provided parameters that all parameters must be within range for A which is not currently enforced.

Use mzed_free_window() to free the window.

Parameters

A	Matrix

lowr	Starting row (inclusive)
lowc	Starting column (inclusive)
highr	End row (exclusive)
highc	End column (exclusive)

3.2.2.14 mzd_slice_t* mzed_slice (mzd_slice_t * *A*, const mzed_t * *Z*)

Unpack the matrix Z into bitslice representation.

Parameters

A	Bitslice matrix or NULL
Z	Input matrix

3.2.2.15 static mzed_t* mzed_stack (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*) [inline], [static]

Stack A on top of B and write the result to C.

That is,

```
[ A ], [ B ] -> [ A ] = C
                [ B ]
```

The inputs are not modified but a new matrix is created.

Parameters

C	Matrix, may be NULL for automatic creation
A	Matrix
B	Matrix

3.2.2.16 static mzed_t* mzed_submatrix (mzed_t * *S*, const mzed_t * *M*, const rci_t *lowr*, const rci_t *lowc*, const rci_t *highr*, const rci_t *highc*) [inline], [static]

Copy a submatrix.

Note that the upper bounds are not included.

Parameters

S	Preallocated space for submatrix, may be NULL for automatic creation.
M	Matrix
lowr	start rows
lowc	start column
highr	stop row (this row is *not* included)
highc	stop column (this column is *not* included)

3.3 Assignment and basic manipulation

Functions

- static void mzd_poly_randomize (mzd_poly_t *A)
  Fill matrix A with random elements.
- void mzd_slice_set_ui (mzd_slice_t *A, word value)
  Return diagonal matrix with value on the diagonal.
- static void mzd_slice_randomize (mzd_slice_t *A)
  Fill matrix A with random elements.
- static mzd_slice_t * mzd_slice_copy (mzd_slice_t *B, const mzd_slice_t *A)
  Copy matrix A to B.
- static word mzd_slice_read_elem (const mzd_slice_t *A, const rci_t row, const rci_t col)
  Get the element at position (row,col) from the matrix A.
- static void mzd_slice_add_elem (mzd_slice_t *A, const rci_t row, const rci_t col, word elem)
  At the element elem to the element at position (row,col) in the matrix A.
- static void mzd_slice_write_elem (mzd_slice_t *A, const rci_t row, const rci_t col, word elem)
  Write the element elem to the position (row,col) in the matrix A.
- void mzed_randomize (mzed_t *A)
  Fill matrix A with random elements.
- mzed_t * mzed_copy (mzed_t *B, const mzed_t *A)
  Copy matrix A to B.
- void mzed_set_ui (mzed_t *A, word value)
  Return diagonal matrix with value on the diagonal.
- static word mzed_read_elem (const mzed_t *A, const rci_t row, const rci_t col)
  Get the element at position (row,col) from the matrix A.
- static void mzed_add_elem (mzed_t *A, const rci_t row, const rci_t col, const word elem)
  At the element elem to the element at position (row,col) in the matrix A.
- static void mzed_write_elem (mzed_t *A, const rci_t row, const rci_t col, const word elem)
  Write the element elem to the position (row,col) in the matrix A.

3.3.1 Detailed Description

3.3.2 Function Documentation

3.3.2.1 static void mzd_poly_randomize (mzd_poly_t * *A*) [inline], [static]

Fill matrix A with random elements.

Parameters

A	Matrix

Todo Allow the user to provide a RNG callback.

3.3.2.2 static void mzd_slice_add_elem (mzd_slice_t * *A*, const rci_t *row*, const rci_t *col*, word *elem*) [inline], [static]

At the element elem to the element at position (row,col) in the matrix A.

Parameters

A	Target matrix.
row	Starting row.
col	Starting column.
elem	finite field element.

Todo This function is considerably slower than it needs to be.

3.3.2.3 static mzd_slice_t* mzd_slice_copy (mzd_slice_t * *B*, const mzd_slice_t * *A*) [inline], [static]

Copy matrix A to B.

Parameters

B	May be NULL for automatic creation.
A	Source matrix.

3.3.2.4 static void mzd_slice_randomize (mzd_slice_t * *A*) [inline], [static]

Fill matrix A with random elements.

Parameters

A	Matrix

Todo Allow the user to provide a RNG callback.

3.3.2.5 static word mzd_slice_read_elem (const mzd_slice_t * *A*, const rci_t *row*, const rci_t *col*) [inline], [static]

Get the element at position (row,col) from the matrix A.

Parameters

A	Source matrix.
row	Starting row.
col	Starting column.

Todo This function is considerably slower than it needs to be.

3.3.2.6 void mzd_slice_set_ui (mzd_slice_t * *A*, word *value*)

Return diagonal matrix with value on the diagonal.

If the matrix is not square then the largest possible square submatrix is used.

Parameters

A	Matrix.
value	Finite Field element.

3.3.2.7 static void mzd_slice_write_elem (mzd_slice_t * *A*, const rci_t *row*, const rci_t *col*, word *elem*) [inline], [static]

Write the element elem to the position (row,col) in the matrix A.

Parameters

A	Target matrix.
row	Starting row.
col	Starting column.
elem	finite field element.

Todo This function is considerably slower than it needs to be.

3.3.2.8 static void mzed_add_elem (mzed_t * *A*, const rci_t *row*, const rci_t *col*, const word *elem*) [inline], [static]

At the element elem to the element at position (row,col) in the matrix A.

Parameters

A	Target matrix.
row	Starting row.
col	Starting column.
elem	finite field element.

3.3.2.9 mzed_t* mzed_copy (mzed_t * *B*, const mzed_t * *A*)

Copy matrix A to B.

Parameters

B	May be NULL for automatic creation.
A	Source matrix.

3.3.2.10 void mzed_randomize (mzed_t * *A*)

Fill matrix A with random elements.

Parameters

A	Matrix

Todo Allow the user to provide a RNG callback.

3.3.2.11 static word mzed_read_elem (const mzed_t * *A*, const rci_t *row*, const rci_t *col*) [inline], [static]

Get the element at position (row,col) from the matrix A.

Parameters

A	Source matrix.
row	Starting row.
col	Starting column.

3.3.2.12 void mzed_set_ui (mzed_t * *A*, word *value*)

Return diagonal matrix with value on the diagonal.

If the matrix is not square then the largest possible square submatrix is used.

Parameters

A	Matrix
value	Finite Field element

3.3.2.13 static void mzed_write_elem (mzed_t * *A*, const rci_t *row*, const rci_t *col*, const word *elem*) [inline], [static]

Write the element elem to the position (row,col) in the matrix A.

Parameters

A	Target matrix.
row	Starting row.
col	Starting column.
elem	finite field element.

3.4 Operations on rows

Functions

- static void mzd_slice_rescale_row (mzd_slice_t ∗A, rci_t r, rci_t c, word x)

  Recale the row r in A by X starting c.
- static void mzd_slice_row_swap (mzd_slice_t ∗A, const rci_t rowa, const rci_t rowb)

  Swap the two rows rowa and rowb.
- static void mzd_slice_copy_row (mzd_slice_t ∗B, size_t i, const mzd_slice_t ∗A, size_t j)

  copy row j from A to row i from B.
- static void mzd_slice_col_swap (mzd_slice_t ∗A, const rci_t cola, const rci_t colb)

  Swap the two columns cola and colb.
- static void mzd_slice_row_add (mzd_slice_t ∗A, const rci_t sourcerow, const rci_t destrow)

  Add the rows sourcerow and destrow and stores the total in the row destrow.
- static void mzd_slice_row_clear_offset (mzd_slice_t ∗A, const rci_t row, const rci_t coloffset)

  Clear the given row, but only begins at the column coloffset.
- void mzed_add_multiple_of_row (mzed_t ∗A, rci_t ar, const mzed_t ∗B, rci_t br, word x, rci_t start_col)
- static void mzed_add_row (mzed_t ∗A, rci_t ar, const mzed_t ∗B, rci_t br, rci_t start_col)
- static void mzed_rescale_row (mzed_t ∗A, rci_t r, rci_t start_col, const word x)

  Rescale the row r in A by X starting c.
- static void mzed_row_swap (mzed_t ∗M, const rci_t rowa, const rci_t rowb)

  Swap the two rows rowa and rowb.
- static void mzed_copy_row (mzed_t ∗B, rci_t i, const mzed_t ∗A, rci_t j)

  copy row j from A to row i from B.
- static void mzed_col_swap (mzed_t ∗M, const rci_t cola, const rci_t colb)

  Swap the two columns cola and colb.
- static void mzed_col_swap_in_rows (mzed_t ∗A, const rci_t cola, const rci_t colb, const rci_t start_row, rci_t stop_row)

  Swap the two columns cola and colb but only between start_row and stop_row.
- static void mzed_row_add (mzed_t ∗M, const rci_t sourcerow, const rci_t destrow)

  Add the rows sourcerow and destrow and stores the total in the row destrow.
- static rci_t mzed_first_zero_row (mzed_t ∗A)

  Return the first row with all zero entries.
- static void mzed_row_clear_offset (mzed_t ∗M, const rci_t row, const rci_t coloffset)

  Clear the given row, but only begins at the column coloffset.
- static void mzed_process_rows (mzed_t ∗M, const rci_t startrow, const rci_t endrow, rci_t startcol, const njt_mzed_t ∗T)

  The function looks up 6 entries from position i,startcol in each row and adds the appropriate row from T to the row i.
- static void mzed_process_rows2 (mzed_t ∗M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t ∗T0, const njt_mzed_t ∗T1)

  Same as mzed_process_rows but works with two Newton-John tables in parallel.
- static void mzed_process_rows3 (mzed_t ∗M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t ∗T0, const njt_mzed_t ∗T1, const njt_mzed_t ∗T2)

  Same as mzed_process_rows but works with three Newton-John tables in parallel.
- static void mzed_process_rows4 (mzed_t ∗M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t ∗T0, const njt_mzed_t ∗T1, const njt_mzed_t ∗T2, const njt_mzed_t ∗T3)

  Same as mzed_process_rows but works with four Newton-John tables in parallel.
- static void mzed_process_rows5 (mzed_t ∗M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t ∗T0, const njt_mzed_t ∗T1, const njt_mzed_t ∗T2, const njt_mzed_t ∗T3, const njt_mzed_t ∗T4)

Same as mzed_process_rows but works with five Newton-John tables in parallel.

- static void mzed_process_rows6 (mzed_t ∗M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t ∗T0, const njt_mzed_t ∗T1, const njt_mzed_t ∗T2, const njt_mzed_t ∗T3, const njt_mzed_t ∗T4, const njt_mzed_t ∗T5)

  Same as mzed_process_rows but works with six Newton-John tables in parallel.

3.4.1 Detailed Description

3.4.2 Function Documentation

3.4.2.1 static void mzd_slice_col_swap (mzd_slice_t ∗ *A*, const rci_t *cola*, const rci_t *colb*) [inline], [static]

Swap the two columns cola and colb.

Parameters

A	Matrix.
cola	Column index.
colb	Column index.

3.4.2.2 static void mzd_slice_copy_row (mzd_slice_t ∗ *B*, size_t *i*, const mzd_slice_t ∗ *A*, size_t *j*) [inline], [static]

copy row j from A to row i from B.

The offsets of A and B must match and the number of columns of A must be less than or equal to the number of columns of B.

Parameters

B	Target matrix.
i	Target row index.
A	Source matrix.
j	Source row index.

3.4.2.3 static void mzd_slice_rescale_row (mzd_slice_t ∗ *A*, rci_t *r*, rci_t *c*, word *x*) [inline], [static]

Recale the row r in A by X starting c.

Parameters

A	Matrix
r	Row index.
c	Column index.
x	Multiplier

3.4.2.4 static void mzd_slice_row_add (mzd_slice_t ∗ *A*, const rci_t *sourcerow*, const rci_t *destrow*) [inline], [static]

Add the rows sourcerow and destrow and stores the total in the row destrow.

Parameters

A	Matrix
sourcerow	Index of source row
destrow	Index of target row

Note

this can be done much faster with mzd_combine.

3.4.2.5 static void mzd_slice_row_clear_offset (mzd_slice_t * *A,* const rci_t *row,* const rci_t *coloffset*) [inline], [static]

Clear the given row, but only begins at the column coloffset.

Parameters

A	Matrix
row	Index of row
coloffset	Column offset

3.4.2.6 static void mzd_slice_row_swap (mzd_slice_t * *A,* const rci_t *rowa,* const rci_t *rowb*) [inline], [static]

Swap the two rows rowa and rowb.

Parameters

A	Matrix
rowa	Row index.
rowb	Row index.

3.4.2.7 void mzed_add_multiple_of_row (mzed_t * *A,* rci_t *ar,* const mzed_t * *B,* rci_t *br,* word *x,* rci_t *start_col*)

A[ar,c] = A[ar,c] + x*B[br,c] for all c >= startcol.

Parameters

A	Matrix.
ar	Row index in A.
B	Matrix.
br	Row index in B.
x	Finite field element.
start_col	Column index.

3.4.2.8 static void mzed_add_row (mzed_t * *A,* rci_t *ar,* const mzed_t * *B,* rci_t *br,* rci_t *start_col*) [inline], [static]

A[ar,c] = A[ar,c] + B[br,c] for all c >= startcol.

Parameters

A	Matrix.

ar	Row index in A.
B	Matrix.
br	Row index in B.
start_col	Column index.

3.4.2.9 static void mzed_col_swap (mzed_t * *M*, const rci_t *cola*, const rci_t *colb*) [inline], [static]

Swap the two columns cola and colb.

Parameters

M	Matrix.
cola	Column index.
colb	Column index.

3.4.2.10 static void mzed_col_swap_in_rows (mzed_t * *A*, const rci_t *cola*, const rci_t *colb*, const rci_t *start_row*, rci_t *stop_row*) [inline], [static]

Swap the two columns cola and colb but only between start_row and stop_row.

Parameters

A	Matrix.
cola	Column index.
colb	Column index.
start_row	Row index.
stop_row	Row index (exclusive).

3.4.2.11 static void mzed_copy_row (mzed_t * *B*, rci_t *i*, const mzed_t * *A*, rci_t *j*) [inline], [static]

copy row j from A to row i from B.

The offsets of A and B must match and the number of columns of A must be less than or equal to the number of columns of B.

Parameters

B	Target matrix.
i	Target row index.
A	Source matrix.
j	Source row index.

3.4.2.12 static rci_t mzed_first_zero_row (mzed_t * *A*) [inline], [static]

Return the first row with all zero entries.

If no such row can be found returns nrows.

Parameters

A	Matrix

3.4.2.13 static void mzed_process_rows (mzed_t * *M*, const rci_t *startrow*, const rci_t *endrow*, rci_t *startcol*, const njt_mzed_t * *T*) [inline], [static]

The function looks up 6 entries from position i,startcol in each row and adds the appropriate row from T to the row i.

This process is iterated for i from startrow to stoprow (exclusive).

Parameters

M	Matrix to operate on
startrow	top row which is operated on
endrow	bottom row which is operated on
startcol	Starting column for addition
T	Newton-John table

3.4.2.14 static void mzed_process_rows2 (mzed_t ∗ *M*, const rci_t *startrow*, const rci_t *endrow*, const rci_t *startcol*, const njt_mzed_t ∗ *T0*, const njt_mzed_t ∗ *T1*) [inline], [static]

Same as mzed_process_rows but works with two Newton-John tables in parallel.

Parameters

M	Matrix to operate on
startrow	top row which is operated on
endrow	bottom row which is operated on
startcol	Starting column for addition
T0	Newton-John table
T1	Newton-John table

3.4.2.15 static void mzed_process_rows3 (mzed_t ∗ *M*, const rci_t *startrow*, const rci_t *endrow*, const rci_t *startcol*, const njt_mzed_t ∗ *T0*, const njt_mzed_t ∗ *T1*, const njt_mzed_t ∗ *T2*) [inline], [static]

Same as mzed_process_rows but works with three Newton-John tables in parallel.

Parameters

M	Matrix to operate on
startrow	top row which is operated on
endrow	bottom row which is operated on
startcol	Starting column for addition
T0	Newton-John table
T1	Newton-John table
T2	Newton-John table

3.4.2.16 static void mzed_process_rows4 (mzed_t ∗ *M*, const rci_t *startrow*, const rci_t *endrow*, const rci_t *startcol*, const njt_mzed_t ∗ *T0*, const njt_mzed_t ∗ *T1*, const njt_mzed_t ∗ *T2*, const njt_mzed_t ∗ *T3*) [inline], [static]

Same as mzed_process_rows but works with four Newton-John tables in parallel.

Parameters

M	Matrix to operate on
startrow	top row which is operated on
endrow	bottom row which is operated on
startcol	Starting column for addition
T0	Newton-John table
T1	Newton-John table

T2	Newton-John table
T3	Newton-John table

3.4.2.17 static void mzed_process_rows5 (mzed_t * *M*, const rci_t *startrow*, const rci_t *endrow*, const rci_t *startcol*, const njt_mzed_t * *T0*, const njt_mzed_t * *T1*, const njt_mzed_t * *T2*, const njt_mzed_t * *T3*, const njt_mzed_t * *T4*) [inline], [static]

Same as mzed_process_rows but works with five Newton-John tables in parallel.

Parameters

M	Matrix to operate on
startrow	top row which is operated on
endrow	bottom row which is operated on
startcol	Starting column for addition
T0	Newton-John table
T1	Newton-John table
T2	Newton-John table
T3	Newton-John table
T4	Newton-John table

3.4.2.18 static void mzed_process_rows6 (mzed_t * *M*, const rci_t *startrow*, const rci_t *endrow*, const rci_t *startcol*, const njt_mzed_t * *T0*, const njt_mzed_t * *T1*, const njt_mzed_t * *T2*, const njt_mzed_t * *T3*, const njt_mzed_t * *T4*, const njt_mzed_t * *T5*) [inline], [static]

Same as mzed_process_rows but works with six Newton-John tables in parallel.

Parameters

M	Matrix to operate on
startrow	top row which is operated on
endrow	bottom row which is operated on
startcol	Starting column for addition
T0	Newton-John table
T1	Newton-John table
T2	Newton-John table
T3	Newton-John table
T4	Newton-John table
T5	Newton-John table

3.4.2.19 static void mzed_rescale_row (mzed_t * *A*, rci_t *r*, rci_t *start_col*, const word *x*) [inline], [static]

Rescale the row r in A by X starting c.

Parameters

A	Matrix
r	Row index.
start_col	Column index.
x	Multiplier

3.4.2.20 static void mzed_row_add (mzed_t * *M*, const rci_t *sourcerow*, const rci_t *destrow*) [inline], [static]

Add the rows sourcerow and destrow and stores the total in the row destrow.

Parameters

M	Matrix
sourcerow	Index of source row
destrow	Index of target row

Note

this can be done much faster with mzed_combine.

3.4.2.21 static void mzed_row_clear_offset (mzed_t * *M*, const rci_t *row*, const rci_t *coloffset*) [inline], [static]

Clear the given row, but only begins at the column coloffset.

Parameters

M	Matrix
row	Index of row
coloffset	Column offset

3.4.2.22 static void mzed_row_swap (mzed_t * *M*, const rci_t *rowa*, const rci_t *rowb*) [inline], [static]

Swap the two rows rowa and rowb.

Parameters

M	Matrix
rowa	Row index.
rowb	Row index.

3.5 String conversions and I/O

Functions

- void mzd_slice_print (const mzd_slice_t ∗A)

  Print a matrix to stdout.
- void mzed_print (const mzed_t ∗M)

  Print a matrix to stdout.

3.5.1 Detailed Description

3.5.2 Function Documentation

3.5.2.1 void mzd_slice_print (const mzd_slice_t ∗ *A*)

Print a matrix to stdout.

Parameters

A	Matrix

3.5.2.2 void mzed_print (const mzed_t ∗ *M*)

Print a matrix to stdout.

Parameters

M	Matrix

3.6 Addition and subtraction

Macros

- #define mzd_slice_sub mzd_slice_add
  $C = A + B$.
- #define _mzd_slice_sub _mzd_slice_add
  $C = A + B$.
- #define mzed_sub mzed_add
  $C = A + B$.
- #define _mzed_sub _mzed_add
  $C = A + B$.

Functions

- static mzd_slice_t * _mzd_slice_add (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)
  $C = A + B$.
- static mzd_slice_t * mzd_slice_add (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)
  $C = A + B$.
- mzed_t * mzed_add (mzed_t *C, const mzed_t *A, const mzed_t *B)
  $C = A + B$.
- mzed_t * _mzed_add (mzed_t *C, const mzed_t *A, const mzed_t *B)
  $C = A + B$.

3.6.1 Detailed Description

3.6.2 Macro Definition Documentation

3.6.2.1 #define _mzd_slice_sub _mzd_slice_add

$C = A + B$.

Parameters

C	Preallocated sum matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.6.2.2 #define _mzed_sub _mzed_add

$C = A + B$.

Parameters

C	Preallocated difference matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.6.2.3 #define mzd_slice_sub mzd_slice_add

$C = A + B$.

C is also returned. If C is NULL then a new matrix is created which must be freed by mzd_slice_free().

Parameters

C	Preallocated sum matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.6.2.4 #define mzed_sub mzed_add

$C = A + B$.

Parameters

C	Preallocated difference matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.6.3 Function Documentation

3.6.3.1 static mzd_slice_t* _mzd_slice_add (mzd_slice_t * C, const mzd_slice_t * A, const mzd_slice_t * B) [inline], [static]

$C = A + B$.

Parameters

C	Preallocated sum matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.6.3.2 mzed_t* _mzed_add (mzed_t * C, const mzed_t * A, const mzed_t * B)

$C = A + B$.

Parameters

C	Preallocated sum matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.6.3.3 static mzd_slice_t* mzd_slice_add (mzd_slice_t * C, const mzd_slice_t * A, const mzd_slice_t * B) [inline], [static]

$C = A + B$.

C is also returned. If C is NULL then a new matrix is created which must be freed by mzd_slice_free().

Parameters

C	Preallocated sum matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.6.3.4 mzed_t* mzed_add (mzed_t * C, const mzed_t * A, const mzed_t * B)

$C = A + B$.

C is also returned. If C is NULL then a new matrix is created which must be freed by mzed_free().

Parameters

C	Preallocated sum matrix, may be NULL for automatic creation.
A	Matrix
B	Matrix

3.7 Multiplication

Functions

- mzd_slice_t ∗ _mzd_slice_mul_naive (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ using quadratic polynomial multiplication with matrix coefficients.
- mzd_slice_t ∗ _mzd_slice_mul_karatsuba2 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ over $\mathbb{F}_{2^2}$ using 3 multiplications over $\mathbb{F}_2$ and 2 temporary $\mathbb{F}_2$ matrices..
- mzd_slice_t ∗ _mzd_slice_mul_karatsuba3 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ over $\mathbb{F}_{2^3}$ using 6 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices..
- mzd_slice_t ∗ _mzd_slice_mul_karatsuba4 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ over $\mathbb{F}_{2^4}$ using 9 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices..
- mzd_slice_t ∗ _mzd_slice_mul_karatsuba5 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ over $\mathbb{F}_{2^5}$ using 13 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices..
- mzd_slice_t ∗ _mzd_slice_mul_karatsuba6 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ over $\mathbb{F}_{2^6}$ using 17 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices.
- mzd_slice_t ∗ _mzd_slice_mul_karatsuba7 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ over $\mathbb{F}_{2^7}$ using 22 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices.
- mzd_slice_t ∗ _mzd_slice_mul_karatsuba8 (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ over $\mathbb{F}_{2^8}$ using 27 multiplications over $\mathbb{F}_2$ and 15 temporary $\mathbb{F}_2$ matrices.
- static mzd_slice_t ∗ _mzd_slice_mul_karatsuba (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = C + A \cdot B$ using Karatsuba multiplication of polynomials over matrices over $\mathbb{F}_2$.
- static mzd_slice_t ∗ mzd_slice_mul_karatsuba (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$ using Karatsuba multiplication of polynomials over matrices over $\mathbb{F}_2$.
- static mzd_slice_t ∗ mzd_slice_addmul_karatsuba (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = C + A \cdot B$ using Karatsuba multiplication of polynomials over matrices over $\mathbb{F}_2$.
- mzd_slice_t ∗ mzd_slice_mul_scalar (mzd_slice_t ∗C, const word a, const mzd_slice_t ∗B)

  $C = a \cdot B$.
- mzd_slice_t ∗ mzd_slice_addmul_scalar (mzd_slice_t ∗C, const word a, const mzd_slice_t ∗B)

  $C += a \cdot B$.
- static mzd_slice_t ∗ mzd_slice_mul (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = A \cdot B$.
- static mzd_slice_t ∗ mzd_slice_addmul (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  $C = C + A \cdot B$.
- mzed_t ∗ mzed_mul (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = A \cdot B$.
- mzed_t ∗ mzed_addmul (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$.
- mzed_t ∗ _mzed_mul (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = A \cdot B$.
- mzed_t ∗ _mzed_addmul (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$.
- mzed_t ∗ mzed_addmul_naive (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$ using naive cubic multiplication.
- mzed_t ∗ mzed_mul_naive (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = A \cdot B$ using naive cubic multiplication.
- mzed_t ∗ _mzed_mul_naive (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

$C = C + A \cdot B$ using naive cubic multiplication.

- mzed_t * mzed_mul_scalar (mzed_t *C, const word a, const mzed_t *B)

  $C = a \cdot B$.
- mzed_t * mzed_mul_newton_john (mzed_t *C, const mzed_t *A, const mzed_t *B)

  $C = A \cdot B$ using Newton-John tables.
- mzed_t * mzed_addmul_newton_john (mzed_t *C, const mzed_t *A, const mzed_t *B)

  $C = C + A \cdot B$ using Newton-John tables.
- mzed_t * _mzed_mul_newton_john0 (mzed_t *C, const mzed_t *A, const mzed_t *B)

  $C = C + A \cdot B$ using Newton-John tables.
- mzed_t * _mzed_mul_newton_john (mzed_t *C, const mzed_t *A, const mzed_t *B)

  $C = C + A \cdot B$ using Newton-John tables.
- mzed_t * mzed_mul_strassen (mzed_t *C, const mzed_t *A, const mzed_t *B, int cutoff)

  $C = A \cdot B$ using Strassen-Winograd.
- mzed_t * mzed_addmul_strassen (mzed_t *C, const mzed_t *A, const mzed_t *B, int cutoff)

  $C = C + A \cdot B$ using Strassen-Winograd.
- mzed_t * _mzed_mul_strassen (mzed_t *C, const mzed_t *A, const mzed_t *B, int cutoff)

  $C = A \cdot B$ using Strassen-Winograd.
- mzed_t * _mzed_addmul_strassen (mzed_t *C, const mzed_t *A, const mzed_t *B, int cutoff)

  $C = A \cdot B$ using Strassen-Winograd.
- rci_t _mzed_strassen_cutoff (const mzed_t *C, const mzed_t *A, const mzed_t *B)

  Return heurstic choice for crossover parameter for Strassen-Winograd multiplication given A, B and C.

3.7.1 Detailed Description

3.7.2 Function Documentation

3.7.2.1 static mzd_slice_t* _mzd_slice_mul_karatsuba (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*) [inline], [static]

$C = C + A \cdot B$ using Karatsuba multiplication of polynomials over matrices over $\mathbb{F}_2$.

This function reduces matrix multiplication over $\mathbb{F}_{2^e}$ to matrix multiplication over $\mathbb{F}_2$.

As an example consider $\mathbb{F}_4$. The minimal polynomial is $x^2 + x + 1$. The matrix A can be represented as A0*x + A1 and the matrix B can be represented as B0*x + B1. Their product C is

$$A0 \cdot B0 \cdot x^2 + (A0 \cdot B1 + A1 \cdot B0) \cdot x + A1 * B1.$$

Reduction modulo x^2 + x + 1 gives

$$(A0 \cdot B0 + A0 \cdot B1 + A1 \cdot B0) \cdot x + A1 \cdot B1 + A0 \cdot B0.$$

This can be re-written as

$$((A0 + A1) \cdot (B0 + B1) + A1 \cdot B1) \cdot x + A1 \cdot B1 + A0 \cdot B0$$

and thus this multiplication costs 3 matrix multiplications over $\mathbb{F}_2$ and 4 matrix additions over $\mathbb{F}_2$.

This technique was proposed in Tomas J. Boothby and Robert W. Bradshaw; Bitslicing and the Method of Four Russians Over Larger Finite Fields; 2009; http://arxiv.org/abs/0901.1413

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

mzed_mul() mzd_slice_mul() mzd_slice_mul_karatsuba()

3.7.2.2 mzd_slice_t* _mzd_slice_mul_karatsuba2 (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*)

$C = A \cdot B$ over $\mathbb{F}_{2^2}$ using 3 multiplications over $\mathbb{F}_2$ and 2 temporary $\mathbb{F}_2$ matrices..

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.3 mzd_slice_t* _mzd_slice_mul_karatsuba3 (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*)

$C = A \cdot B$ over $\mathbb{F}_{2^3}$ using 6 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices..

The formula was taken from Peter L. Montgomery. "Five, Six, and Seven-Term Karatsuba-Like Formulae" in IEEE TRANSACTIONS ON COMPUTERS, VOL. 54, NO. 3, MARCH 2005/

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.4 mzd_slice_t* _mzd_slice_mul_karatsuba4 (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*)

$C = A \cdot B$ over $\mathbb{F}_{2^4}$ using 9 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices..

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.5 mzd_slice_t* _mzd_slice_mul_karatsuba5 (mzd_slice_t * C, const mzd_slice_t * A, const mzd_slice_t * B)

$C = A \cdot B$ over $\mathbb{F}_{2^5}$ using 13 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices..

The formula was taken from Peter L. Montgomery. "Five, Six, and Seven-Term Karatsuba-Like Formulae" in IEEE TRANSACTIONS ON COMPUTERS, VOL. 54, NO. 3, MARCH 2005/

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.6 mzd_slice_t* _mzd_slice_mul_karatsuba6 (mzd_slice_t * C, const mzd_slice_t * A, const mzd_slice_t * B)

$C = A \cdot B$ over $\mathbb{F}_{2^6}$ using 17 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices.

The formula was taken from Peter L. Montgomery. "Five, Six, and Seven-Term Karatsuba-Like Formulae" in IEEE TRANSACTIONS ON COMPUTERS, VOL. 54, NO. 3, MARCH 2005/

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.7 mzd_slice_t* _mzd_slice_mul_karatsuba7 (mzd_slice_t * C, const mzd_slice_t * A, const mzd_slice_t * B)

$C = A \cdot B$ over $\mathbb{F}_{2^7}$ using 22 multiplications over $\mathbb{F}_2$ and 3 temporary $\mathbb{F}_2$ matrices.

The formula was taken from Peter L. Montgomery. "Five, Six, and Seven-Term Karatsuba-Like Formulae" in IEEE TRANSACTIONS ON COMPUTERS, VOL. 54, NO. 3, MARCH 2005/

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.8 mzd_slice_t* _mzd_slice_mul_karatsuba8 (mzd_slice_t * C, const mzd_slice_t * A, const mzd_slice_t * B)

$C = A \cdot B$ over $\mathbb{F}_{2^8}$ using 27 multiplications over $\mathbb{F}_2$ and 15 temporary $\mathbb{F}_2$ matrices.

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

8 + 7 temporaries

Todo reduce memory requirements by writing formula explicitly

3.7.2.9 mzd_slice_t* _mzd_slice_mul_naive (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*)

$C = A \cdot B$ using quadratic polynomial multiplication with matrix coefficients.

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

3.7.2.10 mzed_t* _mzed_addmul (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = C + A \cdot B$.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.

3.7.2.11 mzed_t* _mzed_addmul_strassen (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*, int *cutoff*)

$C = A \cdot B$ using Strassen-Winograd.

This function uses Strassen-Winograd multiplication (Bodrato variant) recursively until it reaches the cutoff, where it switches to Newton-John table based multiplication or naive multiplication.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.
cutoff	Crossover to basecase dimension > 64

Note

See Marco Bodrato; "A Strassen-like Matrix Multiplication Suited for Squaring and Highest Power Computation"; `http://bodrato.it/papres/#CIVV2008` for reference on the used sequence of operations.

3.7.2.12 mzed_t* _mzed_mul (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = A \cdot B$.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.

3.7.2.13 mzed_t* _mzed_mul_naive (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = C + A \cdot B$ using naive cubic multiplication.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.

3.7.2.14 mzed_t* _mzed_mul_newton_john (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = C + A \cdot B$ using Newton-John tables.

This is an optimised implementation.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.

See Also

mzed_mul()

3.7.2.15 mzed_t* _mzed_mul_newton_john0 (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = C + A \cdot B$ using Newton-John tables.

This is a simple implementation for clarity of presentation. Do not call, it is slow.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.

See Also

mzed_mul_newton_john() mzed_mul()

3.7.2.16 mzed_t* _mzed_mul_strassen (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*, int *cutoff*)

$C = A \cdot B$ using Strassen-Winograd.

This function uses Strassen-Winograd multiplication (Bodrato variant) recursively until it reaches the cutoff, where it switches to Newton-John table based multiplication or naive multiplication.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.
cutoff	Crossover to basecase dimension $>$ 64

Note

See Marco Bodrato; "A Strassen-like Matrix Multiplication Suited for Squaring and Highest Power Computation"; http://bodrato.it/papres/#CIVV2008 for reference on the used sequence of operations.

3.7.2.17 rci_t _mzed_strassen_cutoff (const mzed_t ∗ C, const mzed_t ∗ A, const mzed_t ∗ B)

Return heurstic choice for crossover parameter for Strassen-Winograd multiplication given A, B and C.

Parameters

C	Matrix (ignored)
A	Matrix
B	Martix (ignored)

3.7.2.18 static mzd_slice_t∗ mzd_slice_addmul (mzd_slice_t ∗ C, const mzd_slice_t ∗ A, const mzd_slice_t ∗ B) [inline], [static]

$C = C + A \cdot B$.

Parameters

C	Preallocated return matrix.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.19 static mzd_slice_t∗ mzd_slice_addmul_karatsuba (mzd_slice_t ∗ C, const mzd_slice_t ∗ A, const mzd_slice_t ∗ B) [inline], [static]

$C = C + A \cdot B$ using Karatsuba multiplication of polynomials over matrices over $\mathbb{F}_2$.

Parameters

C	Preallocated return matrix.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.20 mzd_slice_t∗ mzd_slice_addmul_scalar (mzd_slice_t ∗ C, const word a, const mzd_slice_t ∗ B)

$C += a \cdot B$.

Parameters

C	Preallocated product matrix.
a	finite field element.
B	Input matrix B.

3.7.2.21 static mzd_slice_t* mzd_slice_mul (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*) [inline], [static]

$C = A \cdot B$.

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.22 static mzd_slice_t* mzd_slice_mul_karatsuba (mzd_slice_t * *C*, const mzd_slice_t * *A*, const mzd_slice_t * *B*) [inline], [static]

$C = A \cdot B$ using Karatsuba multiplication of polynomials over matrices over $\mathbb{F}_2$.

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba()

3.7.2.23 mzd_slice_t* mzd_slice_mul_scalar (mzd_slice_t * *C*, const word *a*, const mzd_slice_t * *B*)

$C = a \cdot B$.

Parameters

C	Preallocated product matrix or NULL.
a	finite field element.
B	Input matrix B.

3.7.2.24 mzed_t* mzed_addmul (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = C + A \cdot B$.

Parameters

C	Preallocated product matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

3.7.2.25 mzed_t* mzed_addmul_naive (mzed_t * C, const mzed_t * A, const mzed_t * B)

$C = C + A \cdot B$ using naive cubic multiplication.

Parameters

C	Preallocated product matrix.
A	Input matrix A.
B	Input matrix B.

Note

There is no reason to call this function except for checking the correctness of other algorithms. It is very slow.

3.7.2.26 mzed_t* mzed_addmul_newton_john (mzed_t * C, const mzed_t * A, const mzed_t * B)

$C = C + A \cdot B$ using Newton-John tables.

Parameters

C	Preallocated product matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzed_mul_newton_john() mzed_mul()

3.7.2.27 mzed_t* mzed_addmul_strassen (mzed_t * C, const mzed_t * A, const mzed_t * B, int cutoff)

$C = C + A \cdot B$ using Strassen-Winograd.

This function uses Strassen-Winograd multiplication (Bodrato variant) recursively until it reaches the cutoff, where it switches to Newton-John table based multiplication or naive multiplication.

Parameters

C	Preallocated product matrix, may be NULL for allocation.
A	Input matrix A.
B	Input matrix B.
cutoff	Crossover to basecase dimension > 64 or 0 for heuristic choice.

3.7.2.28 mzed_t* mzed_mul (mzed_t * C, const mzed_t * A, const mzed_t * B)

$C = A \cdot B$.

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

3.7.2.29 mzed_t* mzed_mul_naive (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = A \cdot B$ using naive cubic multiplication.

Parameters

C	Preallocated product matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

Note

There is no reason to call this function except for checking the correctness of other algorithms. It is very slow.

3.7.2.30 mzed_t* mzed_mul_newton_john (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*)

$C = A \cdot B$ using Newton-John tables.

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

mzed_mul _mzed_mul_newton_john0()

3.7.2.31 mzed_t* mzed_mul_scalar (mzed_t * *C*, const word *a*, const mzed_t * *B*)

$C = a \cdot B$.

Parameters

C	Preallocated product matrix or NULL.
a	finite field element.
B	Input matrix B.

The algorithm proceeds as follows:

0) If a direct approach would need less lookups we use that.

1) We generate a lookup table of 16-bit wide entries

2) We use that lookup table to do 4 lookups per word

3.7.2.32 mzed_t* mzed_mul_strassen (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*, int *cutoff*)

$C = A \cdot B$ using Strassen-Winograd.

This function uses Strassen-Winograd multiplication (Bodrato variant) recursively until it reaches the cutoff, where it switches to Newton-John table based multiplication or naive multiplication.

Parameters

C	Preallocated product matrix, may be NULL for allocation.
A	Input matrix A.
B	Input matrix B.
cutoff	Crossover to basecase dimension $>$ 64 or 0 for heuristic choice

3.8 PLE and PLUQ decomposition

Functions

- rci_t mzed_ple_newton_john (mzed_t *A, mzp_t *P, mzp_t *Q)
  PLE decomposition: $L \cdot E = P \cdot A$ *using Newton-John tables.*
- rci_t mzed_ple_naive (mzed_t *A, mzp_t *P, mzp_t *Q)
  PLE decomposition: $L \cdot E = P \cdot A$.
- rci_t _mzd_slice_ple (mzd_slice_t *A, mzp_t *P, mzp_t *Q, rci_t cutoff)
  PLE decomposition: $L \cdot E = P \cdot A$.
- static rci_t mzd_slice_ple (mzd_slice_t *A, mzp_t *P, mzp_t *Q)
  PLE decomposition: $L \cdot E = P \cdot A$.
- rci_t _mzd_slice_pluq (mzd_slice_t *A, mzp_t *P, mzp_t *Q, rci_t cutoff)
  PLUQ decomposition: $L \cdot U \cdot Q = P \cdot A$.
- static rci_t mzd_slice_pluq (mzd_slice_t *A, mzp_t *P, mzp_t *Q)
  PLUQ decomposition: $L \cdot U \cdot Q = P \cdot A$.
- rci_t _mzed_ple (mzed_t *A, mzp_t *P, mzp_t *Q, rci_t cutoff)
  PLE decomposition: $L \cdot E = P \cdot A$.
- static rci_t mzed_ple (mzed_t *A, mzp_t *P, mzp_t *Q)
  PLE decomposition: $L \cdot E = P \cdot A$.

3.8.1 Detailed Description

3.8.2 Function Documentation

3.8.2.1 rci_t _mzd_slice_ple (mzd_slice_t * *A*, mzp_t * *P*, mzp_t * *Q*, rci_t *cutoff*)

PLE decomposition: $L \cdot E = P \cdot A$.

Modifies A in place to store lower triangular L below (and on) the main diagonal and E – an echelon form of A – above the main diagonal (pivots are stored in Q). P and Q are updated with row and column permutations respectively.

This function uses either asymptotically fast PLE decomposition by reducing it to matrix multiplication or naive cubic PLE decomposition depending on the size of the underlying field. If asymptotically fast PLE decomposition is used, then the algorithm switches to mzed_ple_newton_john if e * ncols * nrows is <= cutoff where e is the exponent of the finite field.

Parameters

A	Matrix
P	Permutation vector of length A->nrows
Q	Permutation vector of length A->ncols
cutoff	Integer

See Also

mzed_ple_naive() mzed_ple_newton_john() mzed_ple()

3.8.2.2 rci_t _mzd_slice_pluq (mzd_slice_t * *A*, mzp_t * *P*, mzp_t * *Q*, rci_t *cutoff*)

PLUQ decomposition: $L \cdot U \cdot Q = P \cdot A$.

This function implements asymptotically fast PLE decomposition by reducing it to matrix multiplication. From PLE the PLUQ decomposition is then obtained.

Parameters

A	Matrix
P	Permutation vector of length A->nrows
Q	Permutation vector of length A->ncols
cutoff	Crossover to base case if mzed_t::w $*$ mzed_t::ncols $*$ mzed_t::nrows $<$ cutoff.

3.8.2.3 rci_t _mzed_ple (mzed_t * *A*, mzp_t * *P*, mzp_t * *Q*, rci_t *cutoff*)

PLE decomposition: $L \cdot E = P \cdot A$.

Modifies A in place to store lower triangular L below (and on) the main diagonal and E – an echelon form of A – above the main diagonal (pivots are stored in Q). P and Q are updated with row and column permutations respectively.

This function uses either asymptotically fast PLE decomposition by reducing it to matrix multiplication or naive cubic PLE decomposition depending on the size of the underlying field. If asymptotically fast PLE decomposition is used, then the algorithm switches to mzed_ple_newton_john if e $*$ ncols $*$ nrows is $<=$ cutoff where e is the exponent of the finite field.

Parameters

A	Matrix
P	Permutation vector of length A->nrows
Q	Permutation vector of length A->ncols
cutoff	Integer >= 0

See Also

mzed_ple_naive() mzed_ple_newton_john() _mzed_ple()

3.8.2.4 static rci_t mzd_slice_ple (mzd_slice_t * *A*, mzp_t * *P*, mzp_t * *Q*) [inline], [static]

PLE decomposition: $L \cdot E = P \cdot A$.

Modifies A in place to store lower triangular L below (and on) the main diagonal and E – an echelon form of A – above the main diagonal (pivots are stored in Q). P and Q are updated with row and column permutations respectively.

This function implements asymptotically fast PLE decomposition by reducing it to matrix multiplication.

Parameters

A	Matrix
P	Permutation vector of length A->nrows
Q	Permutation vector of length A->ncols

See Also

mzed_ple_naive() mzed_ple_newton_john() _mzd_slice_ple()

3.8.2.5 static rci_t mzd_slice_pluq (mzd_slice_t * *A*, mzp_t * *P*, mzp_t * *Q*) [inline], [static]

PLUQ decomposition: $L \cdot U \cdot Q = P \cdot A$.

This function implements asymptotically fast PLE decomposition by reducing it to matrix multiplication. From PLE the PLUQ decomposition is then obtained.

Parameters

A	Matrix
P	Permutation vector of length A->nrows
Q	Permutation vector of length A->ncols

3.8.2.6 static rci_t mzed_ple (mzed_t * *A*, mzp_t * *P*, mzp_t * *Q*) [inline], [static]

PLE decomposition: $L \cdot E = P \cdot A$.

Modifies A in place to store lower triangular L below (and on) the main diagonal and E – an echelon form of A – above the main diagonal (pivots are stored in Q). P and Q are updated with row and column permutations respectively.

This function uses either asymptotically fast PLE decomposition by reducing it to matrix multiplication or naive cubic PLE decomposition depending on the size of the underlying field.

Parameters

A	Matrix
P	Permutation vector of length A->nrows
Q	Permutation vector of length A->ncols

See Also

mzed_ple_naive() mzed_ple_newton_john() _mzed_ple()

3.8.2.7 rci_t mzed_ple_naive (mzed_t * *A*, mzp_t * *P*, mzp_t * *Q*)

PLE decomposition: $L \cdot E = P \cdot A$.

Modifies A in place to store lower triangular L below (and on) the main diagonal and E – an echelon form of A – above the main diagonal (pivots are stored in Q). P and Q are updated with row and column permutations respectively.

This function uses naive cubic PLE decomposition depending on the size of the underlying field.

Parameters

A	Matrix
P	Permutation vector of length A->nrows
Q	Permutation vector of length A->ncols

See Also

mzed_ple_newton_john() mzed_ple()

3.9 Echelon forms

Macros

- #define mzd_slice_echelonize mzd_slice_echelonize_ple
  Compute row echelon forms.

Functions

- rci_t mzd_slice_echelonize_ple (mzd_slice_t ∗A, int full)
  Compute row echelon forms using PLE decomposition.
- static rci_t mzed_echelonize_ple (mzed_t ∗A, int full)
  Compute row echelon forms using PLE decomposition.
- rci_t mzed_echelonize (mzed_t ∗A, int full)
  Compute row echelon forms.
- rci_t mzed_echelonize_naive (mzed_t ∗A, int full)
  Gaussian elimination.
- rci_t mzed_echelonize_newton_john (mzed_t ∗A, int full)
  Reduce matrix A to row echelon form using Gauss-Newton-John elimination.

3.9.1 Detailed Description

3.9.2 Macro Definition Documentation

3.9.2.1 #define mzd_slice_echelonize **mzd_slice_echelonize_ple**

Compute row echelon forms.

Compute the (reduced) row echelon form of the matrix A. If full=0, then return the reduced REF.

Parameters

A	Matrix
full	REF or RREF.

3.9.3 Function Documentation

3.9.3.1 rci_t mzd_slice_echelonize_ple (**mzd_slice_t** ∗ ***A,*** int ***full***)

Compute row echelon forms using PLE decomposition.

Compute the (reduced) row echelon form of the matrix A. If full=0, then return the reduced row echelon. This function reduces echelon forms to PLE (or PLUQ) decomposition.

Parameters

A	Matrix
full	REF or RREF.

3.9.3.2 rci_t mzed_echelonize (**mzed_t** ∗ ***A,*** int ***full***)

Compute row echelon forms.

Compute the (reduced) row echelon form of the matrix A. If full=0, then return the reduced row echelon form.

Parameters

A	Matrix
full	REF or RREF.

3.9.3.3 rci_t mzed_echelonize_naive (mzed_t * *A*, int *full*)

Gaussian elimination.

Perform Gaussian elimination on the matrix A. If full=0, then it will do triangular style elimination, and if full=1, it will do Gauss-Jordan style, or full elimination.

Parameters

A	Matrix
full	Gauss-Jordan style or upper unit-triangular form only.

3.9.3.4 rci_t mzed_echelonize_newton_john (mzed_t * *A*, int *full*)

Reduce matrix A to row echelon form using Gauss-Newton-John elimination.

Parameters

A	Matrix to be reduced.
full	If set to true, the reduced row echelon form will be computed.

Todo we don't really compute the upper triangular form yet, we need to implement _mzed_gauss_submatrix() and a better table creation for that.

3.9.3.5 static rci_t mzed_echelonize_ple (mzed_t * *A*, int *full*) [inline], [static]

Compute row echelon forms using PLE decomposition.

Compute the (reduced) row echelon form of the matrix A. If full=0, then return the reduced REF. This function reduces echelon forms to PLE (or PLUQ) decomposition.

Parameters

A	Matrix
full	REF or RREF.

Note

This function converts A to bitslice representation and back. Hence, it uses more memory than using mzed_echelonize_newton_john() or mzd_slice_echelonize_ple()

Examples:

tests/test_elimination.cc.

3.10 Triangular matrices

Functions

- void mzed_trsm_lower_left_newton_john (const mzed_t ∗L, mzed_t ∗B)
  $B = L^{-1} \cdot B$ *using Newton-John tables.*
- void mzd_slice_trsm_lower_left_newton_john (const mzd_slice_t ∗L, mzd_slice_t ∗B)
  $B = L^{-1} \cdot B$ *using Newton-John tables.*
- void mzed_trsm_upper_left_newton_john (const mzed_t ∗U, mzed_t ∗B)
  $B = U^{-1} \cdot B$ *using Newton-John tables.*
- void mzd_slice_trsm_upper_left_newton_john (const mzd_slice_t ∗U, mzd_slice_t ∗B)
  $B = U^{-1} \cdot B$ *using Newton-John tables.*
- void _mzed_trsm_upper_left (const mzed_t ∗U, mzed_t ∗B, const rci_t cutoff)
  $B = U^{-1} \cdot B$
- void mzed_trsm_upper_left_naive (const mzed_t ∗U, mzed_t ∗B)
  $B = U^{-1} \cdot B$
- static void mzed_trsm_upper_left (const mzed_t ∗U, mzed_t ∗B)
  $B = U^{-1} \cdot B$
- void _mzd_slice_trsm_upper_left (const mzd_slice_t ∗U, mzd_slice_t ∗B, const rci_t cutoff)
  $B = U^{-1} \cdot B$
- void mzd_slice_trsm_upper_left_naive (const mzd_slice_t ∗U, mzd_slice_t ∗B)
  $B = U^{-1} \cdot B$
- static void mzd_slice_trsm_upper_left (const mzd_slice_t ∗U, mzd_slice_t ∗B)
  $B = U^{-1} \cdot B$
- void _mzed_trsm_lower_left (const mzed_t ∗L, mzed_t ∗B, const rci_t cutoff)
  $B = L^{-1} \cdot B$
- void mzed_trsm_lower_left_naive (const mzed_t ∗L, mzed_t ∗B)
  $B = L^{-1} \cdot B$
- static void mzed_trsm_lower_left (const mzed_t ∗L, mzed_t ∗B)
  $B = L^{-1} \cdot B$
- void _mzd_slice_trsm_lower_left (const mzd_slice_t ∗L, mzd_slice_t ∗B, const rci_t cutoff)
  $B = L^{-1} \cdot B$
- void mzd_slice_trsm_lower_left_naive (const mzd_slice_t ∗L, mzd_slice_t ∗B)
  $B = L^{-1} \cdot B$
- static void mzd_slice_trsm_lower_left (const mzd_slice_t ∗L, mzd_slice_t ∗B)
  $B = L^{-1} \cdot B$

3.10.1 Detailed Description

3.10.2 Function Documentation

3.10.2.1 void _mzd_slice_trsm_lower_left (const **mzd_slice_t** ∗ *L*, **mzd_slice_t** ∗ *B*, const rci_t *cutoff*)

$B = L^{-1} \cdot B$

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.
cutoff	Crossover dimension to base case.

3.10.2.2 void _mzd_slice_trsm_upper_left (const mzd_slice_t ∗ *U*, mzd_slice_t ∗ *B*, const rci_t *cutoff*)

$B = U^{-1} \cdot B$

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.
cutoff	Crossover dimension to base case.

3.10.2.3 void _mzed_trsm_lower_left (const mzed_t ∗ *L*, mzed_t ∗ *B*, const rci_t *cutoff*)

$B = L^{-1} \cdot B$

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.
cutoff	Crossover dimension to base case.

3.10.2.4 void _mzed_trsm_upper_left (const mzed_t ∗ *U*, mzed_t ∗ *B*, const rci_t *cutoff*)

$B = U^{-1} \cdot B$

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.
cutoff	Crossover dimension to base case.

3.10.2.5 static void mzd_slice_trsm_lower_left (const mzd_slice_t ∗ *L*, mzd_slice_t ∗ *B*) [inline], [static]

$B = L^{-1} \cdot B$

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.6 void mzd_slice_trsm_lower_left_naive (const mzd_slice_t ∗ *L*, mzd_slice_t ∗ *B*)

$B = L^{-1} \cdot B$

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.7 void mzd_slice_trsm_lower_left_newton_john (const mzd_slice_t ∗ *L*, mzd_slice_t ∗ *B*)

$B = L^{-1} \cdot B$ using Newton-John tables.

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.8 static void mzd_slice_trsm_upper_left (const mzd_slice_t * *U*, mzd_slice_t * *B*) [inline], [static]

$B = U^{-1} \cdot B$

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.9 void mzd_slice_trsm_upper_left_naive (const mzd_slice_t * *U*, mzd_slice_t * *B*)

$B = U^{-1} \cdot B$

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.10 void mzd_slice_trsm_upper_left_newton_john (const mzd_slice_t * *U*, mzd_slice_t * *B*)

$B = U^{-1} \cdot B$ using Newton-John tables.

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.11 static void mzed_trsm_lower_left (const mzed_t * *L*, mzed_t * *B*) [inline], [static]

$B = L^{-1} \cdot B$

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.12 void mzed_trsm_lower_left_naive (const mzed_t * *L*, mzed_t * *B*)

$B = L^{-1} \cdot B$

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.13 void mzed_trsm_lower_left_newton_john (const mzed_t * *L*, mzed_t * *B*)

$B = L^{-1} \cdot B$ using Newton-John tables.

Parameters

L	Lower-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.14 static void mzed_trsm_upper_left (const mzed_t $*$ *U*, mzed_t $*$ *B*) [inline], [static]

$B = U^{-1} \cdot B$

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.15 void mzed_trsm_upper_left_naive (const mzed_t $*$ *U*, mzed_t $*$ *B*)

$B = U^{-1} \cdot B$

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.

3.10.2.16 void mzed_trsm_upper_left_newton_john (const mzed_t $*$ *U*, mzed_t $*$ *B*)

$B = U^{-1} \cdot B$ using Newton-John tables.

Parameters

U	Upper-triangular matrix (other entries are ignored).
B	Matrix.

4 Data Structure Documentation

4.1 gf2e_struct Struct Reference

Data Fields

- unsigned int degree
- word minpoly
- word * pow_gen
- word * red
- word ** _mul
- word(* inv)(const gf2e *ff, const word a)
- word(* mul)(const gf2e *ff, const word a, const word b)

4.1.1 Detailed Description

Examples:

tests/test_elimination.cc.

4.1.2 Field Documentation

4.1.2.1 word** gf2e_struct::_mul

mul[a][b] holds $a \cdot b$ for small fields.

4.1.2.2 unsigned int gf2e_struct::degree

The degree e.

Examples:

tests/test_elimination.cc.

4.1.2.3 word(* gf2e_struct::inv)(const gf2e *ff, const word a)

implements a^(-1) for a in $\mathbb{F}_{2^e}$

4.1.2.4 word gf2e_struct::minpoly

Irreducible polynomial of degree e.

Examples:

tests/test_elimination.cc.

4.1.2.5 word(* gf2e_struct::mul)(const gf2e *ff, const word a, const word b)

implements a*b for a in $\mathbb{F}_{2^e}$

4.1.2.6 word* gf2e_struct::pow_gen

pow_gen[i] holds $a^i / < f >$ for a a generator of this field.

4.1.2.7 word* gf2e_struct::red

red[i] holds precomputed reductors for the minpoly.

The documentation for this struct was generated from the following file:

- gf2e.h

4.2 mzd_poly_t Struct Reference

Data Fields

- mzd_t ** **x**
- rci_t nrows
- rci_t ncols
- deg_t depth

4.2.1 Field Documentation

4.2.1.1 deg_t mzd_poly_t::depth

Degree +1

4.2.1.2 rci_t mzd_poly_t::ncols

Number of columns.

4.2.1.3 rci_t mzd_poly_t::nrows

Number of rows.

The documentation for this struct was generated from the following file:

- mzd_poly.h

4.3 mzd_slice_t Struct Reference

Dense matrices over $\mathbb{F}_{2^e}$ represented as slices of matrices over $\mathbb{F}_2$.

```
#include <mzd_slice.h>
```

Data Fields

- mzd_t * x [16]
- rci_t nrows
- rci_t ncols
- unsigned int depth
- const gf2e * finite_field

4.3.1 Detailed Description

Dense matrices over $\mathbb{F}_{2^e}$ represented as slices of matrices over $\mathbb{F}_2$.

This is one of two fundamental data types of this library, the other being mzed_t. For large matrices ($m \times n \times e > L2$) it is advisable to use this data type because multiplication is faster in this representation. Hence, compared to mzed_t one saves the time to convert betwen representations and - more importantly - memory.

4.3.2 Field Documentation

4.3.2.1 unsigned int mzd_slice_t::depth

Number of slices $*$

Note

This value may be greater than finite_field->degree in some situations

4.3.2.2 const gf2e∗ mzd_slice_t::finite_field

A finite field $\mathbb{F}_{2^e}$.

4.3.2.3 rci_t mzd_slice_t::ncols

Number of columns.

4.3.2.4 rci_t mzd_slice_t::nrows

Number of rows.

4.3.2.5 mzd_t∗ mzd_slice_t::x[16]

mzd_slice_t::x[e][i,j] is the e-th bit of the entry A[i,j].

The documentation for this struct was generated from the following file:

- mzd_slice.h

4.4 mzed_t Struct Reference

Dense matrices over $\mathbb{F}_{2^e}$ represented as packed matrices.

```
#include <mzed.h>
```

Data Fields

- mzed_t ∗ x
- const gf2e ∗ finite_field
- rci_t nrows
- rci_t ncols
- wi_t w

4.4.1 Detailed Description

Dense matrices over $\mathbb{F}_{2^e}$ represented as packed matrices.

Examples:

tests/test_elimination.cc.

4.4.2 Field Documentation

4.4.2.1 const gf2e∗ mzed_t::finite_field

A finite field $\mathbb{F}_{2^e}$.

4.4.2.2 rci_t mzed_t::ncols

Number of columns.

4.4.2.3 rci_t mzed_t::nrows

Number of rows.

4.4.2.4 wi_t mzed_t::w

The internal width of elements (must divide 64).

4.4.2.5 mzd_t∗ mzed_t::x

$m \times n$ matrices over $\mathbb{F}_{2^e}$ are represented as $m \times (en)$ matrices over $\mathbb{F}_2$.

The documentation for this struct was generated from the following file:

- mzed.h

4.5 njt_mzed_t Struct Reference

Newton-John table.

```
#include <newton_john.h>
```

Data Fields

- rci_t ∗ L
- mzed_t ∗ M
- mzed_t ∗ T

4.5.1 Detailed Description

Newton-John table.

4.5.2 Field Documentation

4.5.2.1 rci_t* njt_mzed_t::L

A map such that L[a] points to the row where the first entry is a.

4.5.2.2 mzed_t* njt_mzed_t::M

Table of length e with multiples of the input s.t. a^i is the first entry of row i.

4.5.2.3 mzed_t* njt_mzed_t::T

Actual table of length 2^e of all linear combinations of T.

The documentation for this struct was generated from the following file:

- newton_john.h

5 File Documentation

5.1 conversion.h File Reference

Conversion between mzed_t and mzd_slice_t.

```
#include <m4ri/m4ri.h>
#include <m4rie/mzed.h>
#include <m4rie/mzd_slice.h>
```

Functions

- mzed_t * mzed_cling (mzed_t *A, const mzd_slice_t *Z)

  Pack a bitslice matrix into a packed represenation.
- mzd_slice_t * mzed_slice (mzd_slice_t *A, const mzed_t *Z)

  Unpack the matrix Z into bitslice representation.
- mzd_slice_t * _mzed_slice2 (mzd_slice_t *A, const mzed_t *Z)

  Unpack the matrix Z over GF(2^2) into bitslice representation.
- mzd_slice_t * _mzed_slice4 (mzd_slice_t *A, const mzed_t *Z)

  Unpack the matrix Z over $\mathbb{F}_{2^e}$ into bitslice representation.
- mzd_slice_t * _mzed_slice8 (mzd_slice_t *A, const mzed_t *Z)

  Unpack the matrix Z over $\mathbb{F}_{2^e}$ into bitslice representation.
- mzd_slice_t * _mzed_slice16 (mzd_slice_t *A, const mzed_t *Z)

  Unpack the matrix Z over $\mathbb{F}_{2^e}$ into bitslice representation.
- mzed_t * _mzed_cling2 (mzed_t *A, const mzd_slice_t *Z)

  Pack a bitslice matrix into a classical represenation over GF(2^2).
- mzed_t * _mzed_cling4 (mzed_t *A, const mzd_slice_t *Z)

  Pack a bitslice matrix into a classical represenation over $\mathbb{F}_{2^e}$ for $2 < e <= 4$.
- mzed_t * _mzed_cling8 (mzed_t *A, const mzd_slice_t *Z)

  Pack a bitslice matrix into a classical represenation over $\mathbb{F}_{2^e}$ for $4 < e <= 8$.
- mzed_t * _mzed_cling16 (mzed_t *A, const mzd_slice_t *Z)

  Pack a bitslice matrix into a classical represenation over $\mathbb{F}_{2^e}$ for $8 < e <= 16$.
- static mzed_t * _mzed_mul_karatsuba (mzed_t *C, const mzed_t *A, const mzed_t *B)

*Compute C += A*B using Karatsuba multiplication of polynomials over GF(2).*

- static mzed_t * mzed_mul_karatsuba (mzed_t *C, const mzed_t *A, const mzed_t *B)

  *Compute C = A*B.*
- static mzed_t * mzed_addmul_karatsuba (mzed_t *C, const mzed_t *A, const mzed_t *B)

  *Compute C += A*B.*
- static void mzd_slice_rescale_row (mzd_slice_t *A, rci_t r, rci_t c, word x)

  Recale the row r in A by X starting c.

Variables

- static const word **x80008000** = 0x8000800080008000ULL
- static const word **x80808080** = 0x8080808080808080ULL
- static const word **x88888888** = 0x8888888888888888ULL
- static const word **xaaaaaaaa** = 0xaaaaaaaaaaaaaaaaULL
- static const word **xcccccccc** = 0xccccccccccccccccULL
- static const word **xc0c0c0c0** = 0xc0c0c0c0c0c0c0c0ULL
- static const word **xf0f0f0f0** = 0xf0f0f0f0f0f0f0f0ULL
- static const word **xff00ff00** = 0xff00ff00ff00ff00ULL
- static const word **xffff0000** = 0xffff0000ffff0000ULL
- static const word **xffffffff** = 0xffffffff00000000ULL
- static const word **x__left04** = 0xf000000000000000ULL
- static const word **x__left08** = 0xff00000000000000ULL
- static const word **x__left16** = 0xffff000000000000ULL
- static const word **x__left32** = 0xffffffff00000000ULL

5.1.1 Detailed Description

Conversion between mzed_t and mzd_slice_t.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.1.2 Function Documentation

5.1.2.1 mzed_t* _mzed_cling16 (mzed_t * *A*, const mzd_slice_t * *Z*)

Pack a bitslice matrix into a classical represenation over $\mathbb{F}_{2^e}$ for 8 < e <= 16.

Parameters

A	Matrix over $\mathbb{F}_{2^e}$, must be zero
Z	Bitslice matrix over $\mathbb{F}_{2^e}$

5.1.2.2 mzed_t* _mzed_cling2 (mzed_t * *A*, const mzd_slice_t * *Z*)

Pack a bitslice matrix into a classical represenation over GF(2^2).

Elements in GF(2^2) can be represented as c_1*a + c_0 where a is a root of x^2 + x + 1. A1 contains the coefficients for c_1 while A0 contains the coefficients for c_0.

Parameters

A	Matrix over GF(2^2), must be zero
Z	Bitslice matrix over GF(2^2)

5.1.2.3 mzed_t* _mzed_cling4 (mzed_t * *A*, const mzd_slice_t * *Z*)

Pack a bitslice matrix into a classical represenation over $\mathbb{F}_{2^e}$ for 2 < e <= 4.

Parameters

A	Matrix over $\mathbb{F}_{2^e}$, must be zero
Z	Bitslice matrix over $\mathbb{F}_{2^e}$

5.1.2.4 mzed_t* _mzed_cling8 (mzed_t * *A*, const mzd_slice_t * *Z*)

Pack a bitslice matrix into a classical represenation over $\mathbb{F}_{2^e}$ for 4 < e <= 8.

Parameters

A	Matrix over $\mathbb{F}_{2^e}$, must be zero
Z	Bitslice matrix over $\mathbb{F}_{2^e}$

5.1.2.5 static mzed_t* _mzed_mul_karatsuba (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*) [inline], [static]

Compute C += A*B using Karatsuba multiplication of polynomials over GF(2).

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba

5.1.2.6 mzd_slice_t* _mzed_slice16 (mzd_slice_t * *A*, const mzed_t * *Z*)

Unpack the matrix Z over $\mathbb{F}_{2^e}$ into bitslice representation.

Parameters

A	Zero bitslice matrix over $\mathbb{F}_{2^e}$
Z	Matrix over $\mathbb{F}_{2^e}$

5.1.2.7 mzd_slice_t* _mzed_slice2 (mzd_slice_t * *A*, const mzed_t * *Z*)

Unpack the matrix Z over GF(2^2) into bitslice representation.

Elements in GF(2^2) can be represented as x*a + y where a is a root of x^2 + x + 1. A0 contains the coefficients for x while A1 contains the coefficients for y.

Parameters

A	Zero bitslice matrix over GF(2^2)
Z	Matrix over GF(2^2)

5.1.2.8 mzd_slice_t* _mzed_slice4 (mzd_slice_t * *A*, const mzed_t * *Z*)

Unpack the matrix Z over $\mathbb{F}_{2^e}$ into bitslice representation.

Parameters

A	Zero bitslice matrix over $\mathbb{F}_{2^e}$
Z	Matrix over $\mathbb{F}_{2^e}$

5.1.2.9 mzd_slice_t* _mzed_slice8 (mzd_slice_t * *A*, const mzed_t * *Z*)

Unpack the matrix Z over $\mathbb{F}_{2^e}$ into bitslice representation.

Parameters

A	Zero bitslice matrix over $\mathbb{F}_{2^e}$
Z	Matrix over $\mathbb{F}_{2^e}$

5.1.2.10 static mzed_t* mzed_addmul_karatsuba (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*) `[inline]`, `[static]`

Compute C += A*B.

Parameters

C	Preallocated return matrix.
A	Input matrix A.
B	Input matrix B.

5.1.2.11 static mzed_t* mzed_mul_karatsuba (mzed_t * *C*, const mzed_t * *A*, const mzed_t * *B*) `[inline]`, `[static]`

Compute C = A*B.

Parameters

C	Preallocated return matrix, may be NULL for automatic creation.
A	Input matrix A.
B	Input matrix B.

See Also

_mzd_slice_mul_karatsuba

5.2 echelonform.h File Reference

Echelon forms.

```
#include <m4rie/mzed.h>
#include <m4rie/mzd_slice.h>
#include <m4rie/conversion.h>
```

Macros

- #define mzd_slice_echelonize mzd_slice_echelonize_ple

    Compute row echelon forms.

Functions

- rci_t mzd_slice_echelonize_ple (mzd_slice_t ∗A, int full)

    Compute row echelon forms using PLE decomposition.
- static rci_t mzed_echelonize_ple (mzed_t ∗A, int full)

    Compute row echelon forms using PLE decomposition.
- rci_t mzed_echelonize (mzed_t ∗A, int full)

    Compute row echelon forms.

5.2.1 Detailed Description

Echelon forms.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.3 gf2e.h File Reference

$\mathbb{F}_{2^e}$

```
#include <m4ri/m4ri.h>
#include <m4rie/gf2x.h>
```

Data Structures

- struct gf2e_struct

Macros

- #define **M4RIE_MAX_DEGREE** 16

Typedefs

- typedef struct gf2e_struct gf2e

    $\mathbb{F}_{2^e}$

Functions

- gf2e ∗ gf2e_init (const word minpoly)
- void gf2e_free (gf2e ∗ff)
- static word gf2e_inv (const gf2e ∗ff, word a)

  a^(-1) % minpoly
- static word _gf2e_mul_table (const gf2e ∗ff, const word a, const word b)

  a∗b in $\mathbb{F}_{2^e}$ using a table lookups.
- static word _gf2e_mul_arith (const gf2e ∗ff, const word a, const word b)

  a∗b in $\mathbb{F}_{2^e}$ using a gf2x_mul() lookups.
- static word gf2e_mul (const gf2e ∗ff, const word a, const word b)

  a∗b in $\mathbb{F}_{2^e}$.
- static size_t gf2e_degree_to_w (const gf2e ∗ff)
- static word ∗ gf2e_t16_init (const gf2e ∗ff, const word a)
- static void gf2e_t16_free (word ∗mul)

  Free multiplication table.

Variables

- const word ∗ **irreducible_polynomials** [17]

5.3.1 Detailed Description

$\mathbb{F}_{2^e}$

Author

Martin Albrecht martinralbrecht@googlemail.com

5.3.2 Function Documentation

5.3.2.1 static size_t gf2e_degree_to_w (const gf2e ∗ *ff*) [inline], [static]

Return the width used for storing elements of ff

Parameters

ff	Finite field.

5.3.2.2 void gf2e_free (gf2e ∗ *ff*)

Free ff

Parameters

ff	Finite field.

Examples:

tests/test_elimination.cc.

5.3.2.3 gf2e∗ gf2e_init (const word *minpoly*)

Create finite field from minimal polynomial

Parameters

minpoly	Polynomial represented as series of bits.

red

pow_gen: X^i

mul tables

Examples:

tests/test_elimination.cc.

5.3.2.4 static void gf2e_t16_free (word ∗ *mul*) [inline], [static]

Free multiplication table.

Parameters

mul	Multiplication table

5.3.2.5 static word∗ gf2e_t16_init (const gf2e ∗ *ff*, const word *a*) [inline], [static]

Compute all multiples by a of vectors fitting into 16 bits.

Parameters

ff	Finite field.
a	Finite field element.

Todo : this is a bit of overkill, we could do better

5.4 gf2x.h File Reference

$\mathbb{F}_{2^x}$ for degrees < 64

`#include <m4ri/m4ri.h>`

Macros

- #define __M4RIE_1tF(X) ∼((X)-1)

Functions

- static word gf2x_mul (const word a, const word b, unsigned int d)

  a∗b in $\mathbb{F}_{2^x}$ with deg(a) and deg(b) $< d$.
- static int gf2x_deg (word a)

  deg(a) in $\mathbb{F}_{2^x}$.
- static word gf2x_div (word a, word b)

  a / b in $\mathbb{F}_{2^x}$.
- static word gf2x_mod (word a, word b)

  a mod b in $\mathbb{F}_{2^x}$.
- static word gf2x_divmod (word a, word b, word ∗rem)

a / b and a mod b in $\mathbb{F}_{2^x}$.

- static word gf2x_invmod (word a, word b, unsigned int d)

  a^(-1) % b with deg(a), deg(b) <= d.

5.4.1 Detailed Description

$\mathbb{F}_{2^x}$ for degrees < 64

Author

Martin Albrecht martinralbrecht@googlemail.com

Warning

Do not rely on these functions for high performance, they are not fully optimised.

5.4.2 Macro Definition Documentation

5.4.2.1 #define __M4RIE_1tF(*X*) ~((X)-1)

Maps 1 to word with all ones and 0 to 0.

5.4.3 Function Documentation

5.4.3.1 static int gf2x_deg (word *a*) [inline], [static]

deg(a) in $\mathbb{F}_{2^x}$.

Parameters

a	Polynomial of degree <= 64.

5.5 m4rie.h File Reference

Main include file for the M4RIE library.

```
#include <m4rie/gf2e.h>
#include <m4rie/mzed.h>
#include <m4rie/newton_john.h>
#include <m4rie/echelonform.h>
#include <m4rie/strassen.h>
#include <m4rie/mzd_slice.h>
#include <m4rie/trsm.h>
#include <m4rie/ple.h>
#include <m4rie/conversion.h>
#include <m4rie/permutation.h>
#include <m4rie/mzd_poly.h>
```

5.5.1 Detailed Description

Main include file for the M4RIE library.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.6 mzd_slice.h File Reference

Matrices using a bitsliced representation.

```
#include <m4ri/m4ri.h>
#include <m4rie/mzd_poly.h>
#include <m4rie/mzed.h>
```

Data Structures

- struct mzd_slice_t

  Dense matrices over $\mathbb{F}_{2^e}$ represented as slices of matrices over $\mathbb{F}_2$.

Macros

- #define mzd_slice_sub mzd_slice_add

  $C = A + B$.
- #define _mzd_slice_sub _mzd_slice_add

  $C = A + B$.

Functions

- static mzd_slice_t ∗ mzd_slice_init (const gf2e ∗ff, const rci_t m, const rci_t n)

  Create a new matrix of dimension $m \times n$ over ff.
- void mzd_slice_set_ui (mzd_slice_t ∗A, word value)

  Return diagonal matrix with value on the diagonal.
- static mzd_slice_t ∗ _mzd_slice_adapt_depth (mzd_slice_t ∗A, const unsigned int new_depth)

  Extend or truncate the depth of A to depth new_depth.
- static void mzd_slice_free (mzd_slice_t ∗A)

  Free a matrix created with mzd_slice_init().
- static mzd_slice_t ∗ mzd_slice_concat (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  Concatenate B to A and write the result to C.
- static mzd_slice_t ∗ mzd_slice_stack (mzd_slice_t ∗C, const mzd_slice_t ∗A, const mzd_slice_t ∗B)

  Stack A on top of B and write the result to C.
- static mzd_slice_t ∗ mzd_slice_submatrix (mzd_slice_t ∗S, const mzd_slice_t ∗A, const size_t lowr, const size_t lowc, const size_t highr, const size_t highc)

  Copy a submatrix.
- static mzd_slice_t ∗ mzd_slice_init_window (const mzd_slice_t ∗A, const size_t lowr, const size_t lowc, const size_t highr, const size_t highc)

  Create a window/view into the matrix M.

- static void mzd_slice_free_window (mzd_slice_t *A)

  Free a matrix window created with mzd_slice_init_window().
- static mzd_slice_t * _mzd_slice_add (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A + B$.
- static mzd_slice_t * mzd_slice_add (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A + B$.
- mzd_slice_t * _mzd_slice_mul_naive (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *using quadratic polynomial multiplication with matrix coefficients.*
- mzd_slice_t * _mzd_slice_mul_karatsuba2 (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *over* $\mathbb{F}_{2^2}$ *using 3 multiplications over* $\mathbb{F}_2$ *and 2 temporary* $\mathbb{F}_2$ *matrices..*
- mzd_slice_t * _mzd_slice_mul_karatsuba3 (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *over* $\mathbb{F}_{2^3}$ *using 6 multiplications over* $\mathbb{F}_2$ *and 3 temporary* $\mathbb{F}_2$ *matrices..*
- mzd_slice_t * _mzd_slice_mul_karatsuba4 (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *over* $\mathbb{F}_{2^4}$ *using 9 multiplications over* $\mathbb{F}_2$ *and 3 temporary* $\mathbb{F}_2$ *matrices..*
- mzd_slice_t * _mzd_slice_mul_karatsuba5 (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *over* $\mathbb{F}_{2^5}$ *using 13 multiplications over* $\mathbb{F}_2$ *and 3 temporary* $\mathbb{F}_2$ *matrices..*
- mzd_slice_t * _mzd_slice_mul_karatsuba6 (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *over* $\mathbb{F}_{2^6}$ *using 17 multiplications over* $\mathbb{F}_2$ *and 3 temporary* $\mathbb{F}_2$ *matrices.*
- mzd_slice_t * _mzd_slice_mul_karatsuba7 (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *over* $\mathbb{F}_{2^7}$ *using 22 multiplications over* $\mathbb{F}_2$ *and 3 temporary* $\mathbb{F}_2$ *matrices.*
- mzd_slice_t * _mzd_slice_mul_karatsuba8 (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *over* $\mathbb{F}_{2^8}$ *using 27 multiplications over* $\mathbb{F}_2$ *and 15 temporary* $\mathbb{F}_2$ *matrices.*
- static mzd_slice_t * _mzd_slice_mul_karatsuba (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = C + A \cdot B$ *using Karatsuba multiplication of polynomials over matrices over* $\mathbb{F}_2$.
- static mzd_slice_t * mzd_slice_mul_karatsuba (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$ *using Karatsuba multiplication of polynomials over matrices over* $\mathbb{F}_2$.
- static mzd_slice_t * mzd_slice_addmul_karatsuba (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = C + A \cdot B$ *using Karatsuba multiplication of polynomials over matrices over* $\mathbb{F}_2$.
- mzd_slice_t * mzd_slice_mul_scalar (mzd_slice_t *C, const word a, const mzd_slice_t *B)

  $C = a \cdot B$.
- mzd_slice_t * mzd_slice_addmul_scalar (mzd_slice_t *C, const word a, const mzd_slice_t *B)

  $C += a \cdot B$.
- static mzd_slice_t * mzd_slice_mul (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = A \cdot B$.
- static mzd_slice_t * mzd_slice_addmul (mzd_slice_t *C, const mzd_slice_t *A, const mzd_slice_t *B)

  $C = C + A \cdot B$.
- static void mzd_slice_randomize (mzd_slice_t *A)

  Fill matrix A with random elements.
- static mzd_slice_t * mzd_slice_copy (mzd_slice_t *B, const mzd_slice_t *A)

  Copy matrix A to B.
- static word mzd_slice_read_elem (const mzd_slice_t *A, const rci_t row, const rci_t col)

  Get the element at position (row,col) from the matrix A.
- static void mzd_slice_add_elem (mzd_slice_t *A, const rci_t row, const rci_t col, word elem)

  At the element elem to the element at position (row,col) in the matrix A.
- static void mzd_slice_write_elem (mzd_slice_t *A, const rci_t row, const rci_t col, word elem)

  Write the element elem to the position (row,col) in the matrix A.
- static int mzd_slice_cmp (mzd_slice_t *A, mzd_slice_t *B)

Return -1,0,1 if if A < B, A == B or A > B respectively.

- static int mzd_slice_is_zero (const mzd_slice_t *A)

  Zero test for matrix.
- static void mzd_slice_row_swap (mzd_slice_t *A, const rci_t rowa, const rci_t rowb)

  Swap the two rows rowa and rowb.
- static void mzd_slice_copy_row (mzd_slice_t *B, size_t i, const mzd_slice_t *A, size_t j)

  copy row j from A to row i from B.
- static void mzd_slice_col_swap (mzd_slice_t *A, const rci_t cola, const rci_t colb)

  Swap the two columns cola and colb.
- static void mzd_slice_col_swap_in_rows (mzd_slice_t *A, const rci_t cola, const rci_t colb, const rci_t start_row, rci_t stop_row)

  Swap the two columns cola and colb but only between start_row and stop_row.
- static void mzd_slice_row_add (mzd_slice_t *A, const rci_t sourcerow, const rci_t destrow)

  Add the rows sourcerow and destrow and stores the total in the row destrow.
- static void mzd_slice_row_clear_offset (mzd_slice_t *A, const rci_t row, const rci_t coloffset)

  Clear the given row, but only begins at the column coloffset.
- void mzd_slice_print (const mzd_slice_t *A)

  Print a matrix to stdout.
- static void _mzd_slice_compress_l (mzd_slice_t *A, const rci_t r1, const rci_t n1, const rci_t r2)

  Move the submatrix L of rank r2 starting at column n1 to the left to column r1.

5.6.1 Detailed Description

Matrices using a bitsliced representation. Matrices over $\mathbb{F}_{2^e}$ can be represented as polynomials with matrix coefficients where the matrices are in $\mathbb{F}_2$.

In this file, matrices over $\mathbb{F}_{2^e}$ are implemented as e slices of matrices over $\mathbb{F}_2$ where each slice holds the coefficients of one degree when viewing elements of $\mathbb{F}_{2^e}$ as polynomials over $\mathbb{F}_2$.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.6.2 Function Documentation

5.6.2.1 static mzd_slice_t* _mzd_slice_adapt_depth (mzd_slice_t * *A*, const unsigned int *new_depth*) [inline], [static]

Extend or truncate the depth of A to depth new_depth.

We may think of mzd_slice_t as polynomials over matrices over $\mathbb{F}_2$. This function then truncates/extends these polynomials to degree new_depth-1. In case of extension, all newly created coefficients are zero, hence the mathematical content of A is not changed. In case of truncation higher degree terms are simply deleted and A's mathematical content modified.

Parameters

A	Matrix, modifed in place.

new_depth	Integer >= mzd_slice_t::finite_field::degree.

5.6.2.2 static void _mzd_slice_compress_l (mzd_slice_t * *A*, const rci_t *r1*, const rci_t *n1*, const rci_t *r2*) [inline], [static]

Move the submatrix L of rank r2 starting at column n1 to the left to column r1.

Parameters

A	Matrix
r1	Integer < n1
n1	Integer > r1
r2	Integer <= A->ncols - n1

5.6.2.3 static int mzd_slice_cmp (mzd_slice_t * *A*, mzd_slice_t * *B*) [inline], [static]

Return -1,0,1 if if A < B, A == B or A > B respectively.

Parameters

A	Matrix.
B	Matrix.

Note

This comparison is not well defined (except for !=0) mathematically and relatively arbitrary since elements of G-F(2^k) don't have an ordering.

5.6.2.4 static void mzd_slice_col_swap_in_rows (mzd_slice_t * *A*, const rci_t *cola*, const rci_t *colb*, const rci_t *start_row*, rci_t *stop_row*) [inline], [static]

Swap the two columns cola and colb but only between start_row and stop_row.

Parameters

A	Matrix.
cola	Column index.
colb	Column index.
start_row	Row index.
stop_row	Row index (exclusive).

5.6.2.5 static int mzd_slice_is_zero (const mzd_slice_t * *A*) [inline], [static]

Zero test for matrix.

Parameters

A	Input matrix.

5.7 mzed.h File Reference

Dense matrices over $\mathbb{F}_{2^e}$ represented as packed matrices.

```
#include <m4ri/m4ri.h>
#include <m4rie/gf2e.h>
#include <m4rie/m4ri_functions.h>
```

Data Structures

- struct mzed_t

    Dense matrices over $\mathbb{F}_{2^e}$ represented as packed matrices.

Macros

- #define mzed_sub mzed_add

    $C = A + B$.
- #define _mzed_sub _mzed_add

    $C = A + B$.

Functions

- mzed_t * mzed_init (const gf2e *ff, const rci_t m, const rci_t n)

    Create a new matrix of dimension m x n over ff.
- void mzed_free (mzed_t *A)

    Free a matrix created with mzed_init().
- static mzed_t * mzed_concat (mzed_t *C, const mzed_t *A, const mzed_t *B)

    Concatenate B to A and write the result to C.
- static mzed_t * mzed_stack (mzed_t *C, const mzed_t *A, const mzed_t *B)

    Stack A on top of B and write the result to C.
- static mzed_t * mzed_submatrix (mzed_t *S, const mzed_t *M, const rci_t lowr, const rci_t lowc, const rci_t highr, const rci_t highc)

    Copy a submatrix.
- static mzed_t * mzed_init_window (const mzed_t *A, const rci_t lowr, const rci_t lowc, const rci_t highr, const rci_t highc)

    Create a window/view into the matrix A.
- static void mzed_free_window (mzed_t *A)

    Free a matrix window created with mzed_init_window().
- mzed_t * mzed_add (mzed_t *C, const mzed_t *A, const mzed_t *B)

    $C = A + B$.
- mzed_t * _mzed_add (mzed_t *C, const mzed_t *A, const mzed_t *B)

    $C = A + B$.
- mzed_t * mzed_mul (mzed_t *C, const mzed_t *A, const mzed_t *B)

    $C = A \cdot B$.
- mzed_t * mzed_addmul (mzed_t *C, const mzed_t *A, const mzed_t *B)

    $C = C + A \cdot B$.
- mzed_t * _mzed_mul (mzed_t *C, const mzed_t *A, const mzed_t *B)

    $C = A \cdot B$.
- mzed_t * _mzed_addmul (mzed_t *C, const mzed_t *A, const mzed_t *B)

    $C = C + A \cdot B$.

- mzed_t ∗ mzed_addmul_naive (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$ using naive cubic multiplication.
- mzed_t ∗ mzed_mul_naive (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = A \cdot B$ using naive cubic multiplication.
- mzed_t ∗ _mzed_mul_naive (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$ using naive cubic multiplication.
- mzed_t ∗ mzed_mul_scalar (mzed_t ∗C, const word a, const mzed_t ∗B)

  $C = a \cdot B$.
- mzed_t ∗ _mzed_mul_init (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B, int clear)
- void mzed_randomize (mzed_t ∗A)

  Fill matrix A with random elements.
- mzed_t ∗ mzed_copy (mzed_t ∗B, const mzed_t ∗A)

  Copy matrix A to B.
- void mzed_set_ui (mzed_t ∗A, word value)

  Return diagonal matrix with value on the diagonal.
- static word mzed_read_elem (const mzed_t ∗A, const rci_t row, const rci_t col)

  Get the element at position (row,col) from the matrix A.
- static void mzed_add_elem (mzed_t ∗A, const rci_t row, const rci_t col, const word elem)

  At the element elem to the element at position (row,col) in the matrix A.
- static void mzed_write_elem (mzed_t ∗A, const rci_t row, const rci_t col, const word elem)

  Write the element elem to the position (row,col) in the matrix A.
- static int mzed_cmp (mzed_t ∗A, mzed_t ∗B)

  Return -1,0,1 if if A < B, A == B or A > B respectively.
- static int mzed_is_zero (const mzed_t ∗A)

  Zero test for matrix.
- void mzed_add_multiple_of_row (mzed_t ∗A, rci_t ar, const mzed_t ∗B, rci_t br, word x, rci_t start_col)
- static void mzed_add_row (mzed_t ∗A, rci_t ar, const mzed_t ∗B, rci_t br, rci_t start_col)
- static void mzed_rescale_row (mzed_t ∗A, rci_t r, rci_t start_col, const word x)

  Rescale the row r in A by X starting c.
- static void mzed_row_swap (mzed_t ∗M, const rci_t rowa, const rci_t rowb)

  Swap the two rows rowa and rowb.
- static void mzed_copy_row (mzed_t ∗B, rci_t i, const mzed_t ∗A, rci_t j)

  copy row j from A to row i from B.
- static void mzed_col_swap (mzed_t ∗M, const rci_t cola, const rci_t colb)

  Swap the two columns cola and colb.
- static void mzed_col_swap_in_rows (mzed_t ∗A, const rci_t cola, const rci_t colb, const rci_t start_row, rci_t stop_row)

  Swap the two columns cola and colb but only between start_row and stop_row.
- static void mzed_row_add (mzed_t ∗M, const rci_t sourcerow, const rci_t destrow)

  Add the rows sourcerow and destrow and stores the total in the row destrow.
- static rci_t mzed_first_zero_row (mzed_t ∗A)

  Return the first row with all zero entries.
- static void mzed_row_clear_offset (mzed_t ∗M, const rci_t row, const rci_t coloffset)

  Clear the given row, but only begins at the column coloffset.
- rci_t mzed_echelonize_naive (mzed_t ∗A, int full)

  Gaussian elimination.
- void mzed_print (const mzed_t ∗M)

  Print a matrix to stdout.

5.7.1 Detailed Description

Dense matrices over $\mathbb{F}_{2^e}$ represented as packed matrices. This file implements the data type mzed_t. That is, matrices over $\mathbb{F}_{2^e}$ in row major representation.

For example, let $a = \sum a_i x_i / < f >$ and $b = \sum b_i x_i / < f >$ be elements in $\mathbb{F}_{2^6}$ with minimal polynomial f. Then, the 1×2 matrix [b a] would be stored as

```
[...| 0 0 b5 b4 b3 b2 b1 b0 | 0 0 a5 a4 a3 a2 a1 a0]
```

Internally M4RI matrices are used to store bits with allows to re-use existing M4RI methods (such as mzd_add) when implementing functions for mzed_t.

This data type is preferable when Newton-John tables ought be used or when the matrix is small ($m \times n \times e < L2$).

Author

Martin Albrecht martinralbrecht@googlemail.com

5.7.2 Function Documentation

5.7.2.1 mzed_t∗ _mzed_mul_init (mzed_t ∗ *C*, const mzed_t ∗ *A*, const mzed_t ∗ *B*, int *clear*)

Check whether C, A and B match in sizes and fields for multiplication

Parameters

C	Output matrix, if NULL a new matrix is created.
A	Input matrix.
B	Input matrix.
clear	Write zeros to C or not.

5.7.2.2 static int mzed_cmp (mzed_t ∗ *A*, mzed_t ∗ *B*) [inline], [static]

Return -1,0,1 if if A < B, A == B or A > B respectively.

Parameters

A	Matrix.
B	Matrix.

Note

This comparison is not well defined mathematically and relatively arbitrary since elements of $\mathbb{F}_{2^e}$ don't have an ordering.

Examples:

tests/test_elimination.cc.

5.7.2.3 static int mzed_is_zero (const mzed_t ∗ *A*) [inline], [static]

Zero test for matrix.

Parameters

A	Input matrix.

5.8 newton_john.h File Reference

Newton-John table based algorithms.

```
#include <m4rie/gf2e.h>
#include <m4rie/mzed.h>
#include <m4rie/mzd_slice.h>
```

Data Structures

- struct njt_mzed_t

  Newton-John table.

Functions

- njt_mzed_t ∗ njt_mzed_init (const gf2e ∗ff, const rci_t ncols)

  Allocate Newton-John table of dimension gf2e::degree<<1 ∗ ncols.
- void njt_mzed_free (njt_mzed_t ∗t)

  Free Newton-John table.
- njt_mzed_t ∗ mzed_make_table (njt_mzed_t ∗T, const mzed_t ∗A, const rci_t r, const rci_t c)

  Construct Newton-John table T for row r of A, and element A[r,c].
- mzed_t ∗ mzed_mul_newton_john (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = A \cdot B$ *using Newton-John tables.*
- mzed_t ∗ mzed_addmul_newton_john (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$ *using Newton-John tables.*
- mzed_t ∗ _mzed_mul_newton_john0 (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$ *using Newton-John tables.*
- mzed_t ∗ _mzed_mul_newton_john (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  $C = C + A \cdot B$ *using Newton-John tables.*
- rci_t mzed_echelonize_newton_john (mzed_t ∗A, int full)

  Reduce matrix A to row echelon form using Gauss-Newton-John elimination.
- mzed_t ∗ mzed_invert_newton_john (mzed_t ∗B, const mzed_t ∗A)

  Invert the matrix A using Gauss-Newton-John elimination.
- void mzed_trsm_lower_left_newton_john (const mzed_t ∗L, mzed_t ∗B)

  $B = L^{-1} \cdot B$ *using Newton-John tables.*
- void mzd_slice_trsm_lower_left_newton_john (const mzd_slice_t ∗L, mzd_slice_t ∗B)

  $B = L^{-1} \cdot B$ *using Newton-John tables.*
- void mzed_trsm_upper_left_newton_john (const mzed_t ∗U, mzed_t ∗B)

  $B = U^{-1} \cdot B$ *using Newton-John tables.*
- void mzd_slice_trsm_upper_left_newton_john (const mzd_slice_t ∗U, mzd_slice_t ∗B)

  $B = U^{-1} \cdot B$ *using Newton-John tables.*
- rci_t mzed_ple_newton_john (mzed_t ∗A, mzp_t ∗P, mzp_t ∗Q)

  PLE decomposition: $L \cdot E = P \cdot A$ *using Newton-John tables.*

- static void mzed_process_rows (mzed_t *M, const rci_t startrow, const rci_t endrow, rci_t startcol, const njt_-mzed_t *T)

  The function looks up 6 entries from position i,startcol in each row and adds the appropriate row from T to the row i.
- static void mzed_process_rows2 (mzed_t *M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t *T0, const njt_mzed_t *T1)

  Same as mzed_process_rows but works with two Newton-John tables in parallel.
- static void mzed_process_rows3 (mzed_t *M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t *T0, const njt_mzed_t *T1, const njt_mzed_t *T2)

  Same as mzed_process_rows but works with three Newton-John tables in parallel.
- static void mzed_process_rows4 (mzed_t *M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t *T0, const njt_mzed_t *T1, const njt_mzed_t *T2, const njt_mzed_t *T3)

  Same as mzed_process_rows but works with four Newton-John tables in parallel.
- static void mzed_process_rows5 (mzed_t *M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t *T0, const njt_mzed_t *T1, const njt_mzed_t *T2, const njt_mzed_t *T3, const njt_mzed_t *T4)

  Same as mzed_process_rows but works with five Newton-John tables in parallel.
- static void mzed_process_rows6 (mzed_t *M, const rci_t startrow, const rci_t endrow, const rci_t startcol, const njt_mzed_t *T0, const njt_mzed_t *T1, const njt_mzed_t *T2, const njt_mzed_t *T3, const njt_mzed_t *T4, const njt_mzed_t *T5)

  Same as mzed_process_rows but works with six Newton-John tables in parallel.

5.8.1 Detailed Description

Newton-John table based algorithms.

Note

These tables were formally known as Travolta tables.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.8.2 Function Documentation

5.8.2.1 mzed_t* mzed_invert_newton_john (mzed_t * *B*, const mzed_t * *A*)

Invert the matrix A using Gauss-Newton-John elimination.

Parameters

B	Preallocated space for inversion matrix, may be NULL for automatic creation.
A	Matrix to be inverted.

5.8.2.2 njt_mzed_t* mzed_make_table (njt_mzed_t * *T*, const mzed_t * *A*, const rci_t *r*, const rci_t *c*)

Construct Newton-John table T for row r of A, and element A[r,c].

Parameters

T	Preallocated Newton-John table or NULL.
A	Matrix.
r	Row index.
c	Column index.

5.8.2.3 void njt_mzed_free (njt_mzed_t * *t*)

Free Newton-John table.

Parameters

t	Table

5.8.2.4 njt_mzed_t* njt_mzed_init (const gf2e * *ff*, const rci_t *ncols*)

Allocate Newton-John table of dimension gf2e::degree<<1 ∗ ncols.

Parameters

ff	Finite field.
ncols	Integer > 0.

5.9 permutation.h File Reference

Permutation matrices.

```
#include <m4ri/mzp.h>
#include <m4rie/mzed.h>
#include <m4rie/mzd_slice.h>
```

Functions

- static void mzed_apply_p_left (mzed_t ∗A, mzp_t const ∗P)
- static void mzed_apply_p_left_trans (mzed_t ∗A, mzp_t const ∗P)
- static void mzed_apply_p_right (mzed_t ∗A, mzp_t const ∗P)
- static void mzed_apply_p_right_trans (mzed_t ∗A, mzp_t const ∗P)
- static void mzd_slice_apply_p_left (mzd_slice_t ∗A, mzp_t const ∗P)
- static void mzd_slice_apply_p_left_trans (mzd_slice_t ∗A, mzp_t const ∗P)
- static void mzd_slice_apply_p_right (mzd_slice_t ∗A, mzp_t const ∗P)
- static void mzd_slice_apply_p_right_trans (mzd_slice_t ∗A, mzp_t const ∗P)
- static void mzd_slice_apply_p_right_trans_tri (mzd_slice_t ∗A, mzp_t const ∗P)

5.9.1 Detailed Description

Permutation matrices.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.9.2 Function Documentation

5.9.2.1 static void mzd_slice_apply_p_left (mzd_slice_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the left.

This is equivalent to row swaps walking from 0 to length-1.

Parameters

A	Matrix.
P	Permutation.

5.9.2.2 static void mzd_slice_apply_p_left_trans (mzd_slice_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the left but transpose P before.

This is equivalent to row swaps walking from length-1 to 0.

Parameters

A	Matrix.
P	Permutation.

5.9.2.3 static void mzd_slice_apply_p_right (mzd_slice_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the right.

This is equivalent to column swaps walking from length-1 to 0.

Parameters

A	Matrix.
P	Permutation.

5.9.2.4 static void mzd_slice_apply_p_right_trans (mzd_slice_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the right but transpose P before.

This is equivalent to column swaps walking from 0 to length-1.

Parameters

A	Matrix.
P	Permutation.

5.9.2.5 static void mzd_slice_apply_p_right_trans_tri (mzd_slice_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the right, but only on the upper the matrix A above the main diagonal.

This is equivalent to column swaps walking from 0 to length-1 and is used to compress PLE to PLUQ.

Parameters

A	Matrix.

P	Permutation.

5.9.2.6 static void mzed_apply_p_left (mzed_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the left.

This is equivalent to row swaps walking from 0 to length-1.

Parameters

A	Matrix.
P	Permutation.

5.9.2.7 static void mzed_apply_p_left_trans (mzed_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the left but transpose P before.

This is equivalent to row swaps walking from length-1 to 0.

Parameters

A	Matrix.
P	Permutation.

5.9.2.8 static void mzed_apply_p_right (mzed_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the right.

This is equivalent to column swaps walking from length-1 to 0.

Parameters

A	Matrix.
P	Permutation.

5.9.2.9 static void mzed_apply_p_right_trans (mzed_t * *A*, mzp_t const * *P*) [inline], [static]

Apply the permutation P to A from the right but transpose P before.

This is equivalent to column swaps walking from 0 to length-1.

Parameters

A	Matrix.
P	Permutation.

5.10 ple.h File Reference

PLE decomposition: $L \cdot E = P \cdot A$.

```
#include <m4ri/m4ri.h>
#include <m4rie/mzed.h>
#include <m4rie/mzd_slice.h>
#include <m4rie/conversion.h>
```

Macros

- #define __M4RIE_PLE_CUTOFF (__M4RI_CPU_L2_CACHE<<2)

Functions

- rci_t mzed_ple_naive (mzed_t ∗A, mzp_t ∗P, mzp_t ∗Q)
  PLE decomposition: $L \cdot E = P \cdot A$.
- rci_t _mzd_slice_ple (mzd_slice_t ∗A, mzp_t ∗P, mzp_t ∗Q, rci_t cutoff)
  PLE decomposition: $L \cdot E = P \cdot A$.
- static rci_t mzd_slice_ple (mzd_slice_t ∗A, mzp_t ∗P, mzp_t ∗Q)
  PLE decomposition: $L \cdot E = P \cdot A$.
- rci_t _mzd_slice_pluq (mzd_slice_t ∗A, mzp_t ∗P, mzp_t ∗Q, rci_t cutoff)
  PLUQ decomposition: $L \cdot U \cdot Q = P \cdot A$.
- static rci_t mzd_slice_pluq (mzd_slice_t ∗A, mzp_t ∗P, mzp_t ∗Q)
  PLUQ decomposition: $L \cdot U \cdot Q = P \cdot A$.
- rci_t _mzed_ple (mzed_t ∗A, mzp_t ∗P, mzp_t ∗Q, rci_t cutoff)
  PLE decomposition: $L \cdot E = P \cdot A$.
- static rci_t mzed_ple (mzed_t ∗A, mzp_t ∗P, mzp_t ∗Q)
  PLE decomposition: $L \cdot E = P \cdot A$.

5.10.1 Detailed Description

PLE decomposition: $L \cdot E = P \cdot A$.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.10.2 Macro Definition Documentation

5.10.2.1 #define __M4RIE_PLE_CUTOFF (__M4RI_CPU_L2_CACHE<<2)

Default crossover to PLE base case (Newton-John based).

5.11 strassen.h File Reference

Strassen-Winograd multiplication for mzed_t.

Functions

- mzed_t ∗ mzed_mul_strassen (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B, int cutoff)
  $C = A \cdot B$ *using Strassen-Winograd.*
- mzed_t ∗ mzed_addmul_strassen (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B, int cutoff)
  $C = C + A \cdot B$ *using Strassen-Winograd.*
- mzed_t ∗ _mzed_mul_strassen (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B, int cutoff)
  $C = A \cdot B$ *using Strassen-Winograd.*
- mzed_t ∗ _mzed_addmul_strassen (mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B, int cutoff)

$C = A \cdot B$ using Strassen-Winograd.

- rci_t _mzed_strassen_cutoff (const mzed_t ∗C, const mzed_t ∗A, const mzed_t ∗B)

  Return heurstic choice for crossover parameter for Strassen-Winograd multiplication given A, B and C.

5.11.1 Detailed Description

Strassen-Winograd multiplication for mzed_t.

Author

Martin Albrecht martinralbrecht@googlemail.com

5.12 trsm.h File Reference

Triangular System Solving with Matrices (TRSM).

```
#include <m4rie/mzed.h>
#include <m4rie/mzd_slice.h>
```

Macros

- #define MZED_TRSM_CUTOFF 512

Functions

- void _mzed_trsm_upper_left (const mzed_t ∗U, mzed_t ∗B, const rci_t cutoff)

  $B = U^{-1} \cdot B$
- void mzed_trsm_upper_left_naive (const mzed_t ∗U, mzed_t ∗B)

  $B = U^{-1} \cdot B$
- static void mzed_trsm_upper_left (const mzed_t ∗U, mzed_t ∗B)

  $B = U^{-1} \cdot B$
- void _mzd_slice_trsm_upper_left (const mzd_slice_t ∗U, mzd_slice_t ∗B, const rci_t cutoff)

  $B = U^{-1} \cdot B$
- void mzd_slice_trsm_upper_left_naive (const mzd_slice_t ∗U, mzd_slice_t ∗B)

  $B = U^{-1} \cdot B$
- static void mzd_slice_trsm_upper_left (const mzd_slice_t ∗U, mzd_slice_t ∗B)

  $B = U^{-1} \cdot B$
- void _mzed_trsm_lower_left (const mzed_t ∗L, mzed_t ∗B, const rci_t cutoff)

  $B = L^{-1} \cdot B$
- void mzed_trsm_lower_left_naive (const mzed_t ∗L, mzed_t ∗B)

  $B = L^{-1} \cdot B$
- static void mzed_trsm_lower_left (const mzed_t ∗L, mzed_t ∗B)

  $B = L^{-1} \cdot B$
- void _mzd_slice_trsm_lower_left (const mzd_slice_t ∗L, mzd_slice_t ∗B, const rci_t cutoff)

  $B = L^{-1} \cdot B$
- void mzd_slice_trsm_lower_left_naive (const mzd_slice_t ∗L, mzd_slice_t ∗B)

  $B = L^{-1} \cdot B$
- static void mzd_slice_trsm_lower_left (const mzd_slice_t ∗L, mzd_slice_t ∗B)

  $B = L^{-1} \cdot B$

5.12.1 Detailed Description

Triangular System Solving with Matrices (TRSM).

Author

Martin Albrecht martinralbrecht@googlemail.com

5.12.2 Macro Definition Documentation

5.12.2.1 #define MZED_TRSM_CUTOFF 512

Crossover dimension to TRSM base cases

6 Example Documentation

6.1 tests/test_elimination.cc

tests/test_multiplication.cc

```
/*******************************************************************************
*
*            M4RIE: Linear Algebra over GF(2^e)
*
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*
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*
*                  http://www.gnu.org/licenses/
******************************************************************************/

#include "testing.h"

int test_equality(gf2e *ff, rci_t m, rci_t n) {
  int fail_ret = 0;
  mzed_t *A0 = random_mzed_t(ff, m, n);
  mzed_t *A1 = mzed_copy(NULL, A0);
  mzed_t *A2 = mzed_copy(NULL, A0);
  mzed_t *A3 = mzed_copy(NULL, A0);

  mzed_set_canary(A1);
  mzed_set_canary(A2);
  mzed_set_canary(A3);

  const rci_t r0 = mzed_echelonize_newton_john(A0,1);
  const rci_t r1 = mzed_echelonize_naive(A1,1);
  const rci_t r2 = mzed_echelonize(A2,1);
  const rci_t r3 = mzed_echelonize_ple(A3,1);

  m4rie_check( r0 == r1);
  m4rie_check( mzed_cmp(A0, A1) == 0);

  m4rie_check( r1 == r2);
  m4rie_check( mzed_cmp(A1, A2) == 0);

  m4rie_check( r2 == r3);
  m4rie_check( mzed_cmp(A2, A3) == 0);
  m4rie_check( r3 == r0);
  m4rie_check( mzed_cmp(A3, A0) == 0);
```

```
  m4rie_check( mzed_canary_is_alive(A0) );
  m4rie_check( mzed_canary_is_alive(A1) );
  m4rie_check( mzed_canary_is_alive(A2) );
  m4rie_check( mzed_canary_is_alive(A3) );

  mzed_free(A0);
  mzed_free(A1);
  mzed_free(A2);
  mzed_free(A3);

  return fail_ret;
}

int test_batch(gf2e *ff, rci_t m, rci_t n) {
  int fail_ret = 0;
  printf("elim: k: %2d, minpoly: 0x%05x m: %5d, n: %5d ",(int)ff->degree, (unsigned int)ff->
      minpoly, (int)m, (int)n);

  if(m == n) {
    m4rie_check(   test_equality(ff, m, n) == 0); printf("."); fflush(0);
    printf(" ");
  } else {
    m4rie_check(   test_equality(ff, m, n) == 0); printf("."); fflush(0);
    m4rie_check(   test_equality(ff, n, m) == 0); printf("."); fflush(0);
  }

  if (fail_ret == 0)
    printf(" passed\n");
  else
    printf(" FAILED\n");

  return fail_ret;
}

int main(int argc, char **argv) {
  srandom(17);

  int runlong = parse_parameters(argc, argv);

  gf2e *ff;
  int fail_ret = 0;

  for(int k=2; k<=16; k++) {
    ff = gf2e_init(irreducible_polynomials[k][1]);

    fail_ret += test_batch(ff,   2,   5);
    fail_ret += test_batch(ff,   5,  10);
    fail_ret += test_batch(ff,   1,   1);
    fail_ret += test_batch(ff,   1,   2);
    fail_ret += test_batch(ff,  11,  12);
    fail_ret += test_batch(ff,  21,  22);
    fail_ret += test_batch(ff,  13,   2);
    fail_ret += test_batch(ff,  32,  33);
    fail_ret += test_batch(ff,  63,  64);
    if (k <= 12 || runlong) {
      fail_ret += test_batch(ff, 127, 128);
      fail_ret += test_batch(ff, 200,  20);
    }
    fail_ret += test_batch(ff,   1,   1);
    fail_ret += test_batch(ff,   1,   3);
    fail_ret += test_batch(ff,  11,  13);
    fail_ret += test_batch(ff,  21,  23);
    fail_ret += test_batch(ff,  13,  90);
    fail_ret += test_batch(ff,  32,  34);
    fail_ret += test_batch(ff,  63,  65);
    if (k <= 12 || runlong) {
      fail_ret += test_batch(ff, 127, 129);
      fail_ret += test_batch(ff, 200, 112);
      fail_ret += test_batch(ff,  10, 200);
    }
    gf2e_free(ff);
  }

  return fail_ret;
}
```

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